

Instructions

There are **two** sections in this examination paper.

Section A	Concepts and Skills	150 marks	6 questions
Section B	Contexts and Applications	150 marks	3 questions

Answer **all nine** questions, as follows:

In Section A, answer:

Questions 1 to 5 and
either Question 6A **or** Question 6B.

In Section B, answer Questions 7, 8, and 9.

Write your answers in the spaces provided in this booklet. You may lose marks if you do not do so. There is space for extra work at the back of the booklet. You may also ask the superintendent for more paper. Label any extra work clearly with the question number and part.

The superintendent will give you a copy of the booklet of *Formulae and Tables*. You must return it at the end of the examination. You are not allowed to bring your own copy into the examination.

Marks will be lost if all necessary work is not clearly shown.

Answers should include the appropriate units of measurement, where relevant.

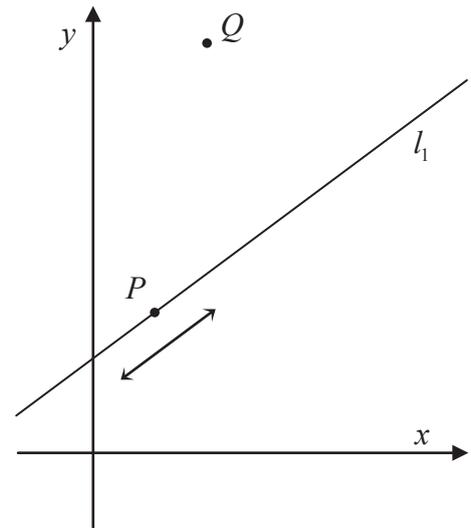
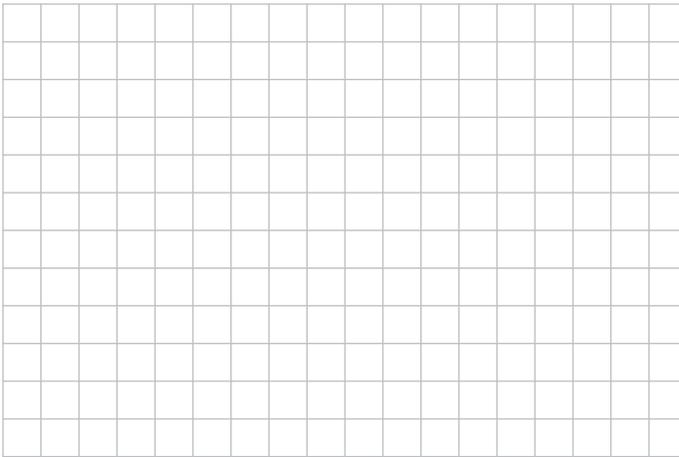
Answers should be given in simplest form, where relevant.

Write the make and model of your calculator(s) here:

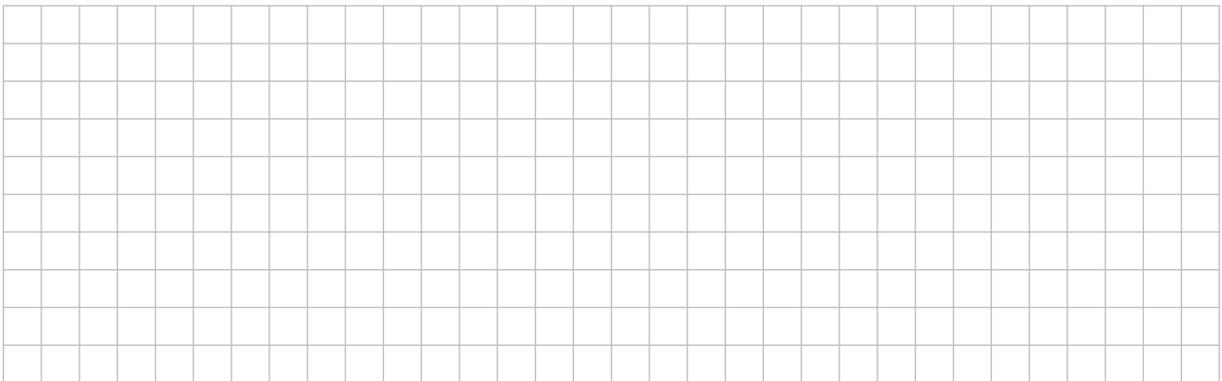
Question 3

(25 marks)

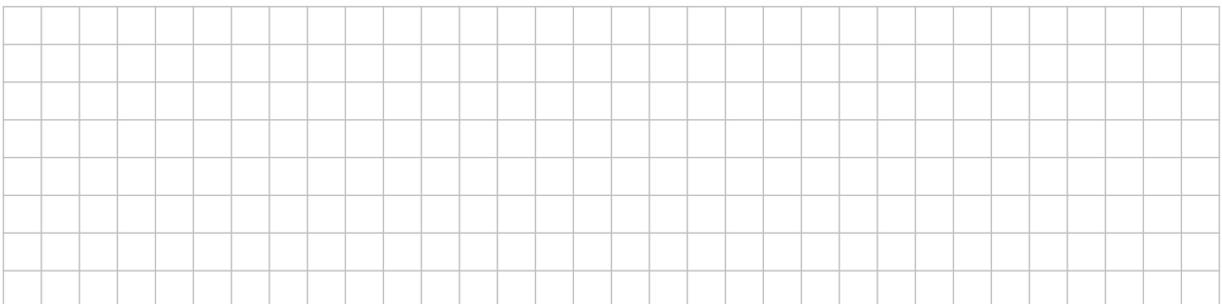
- (a) Show that, for all $k \in \mathbb{R}$, the point $P(4k - 2, 3k + 1)$ lies on the line $l_1 : 3x - 4y + 10 = 0$.



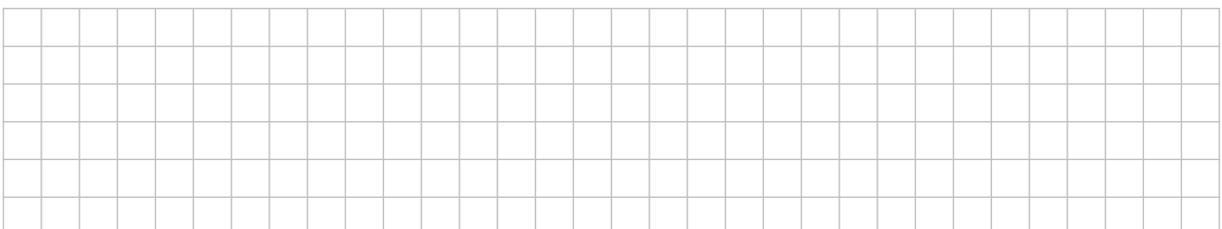
- (b) The line l_2 passes through P and is perpendicular to l_1 . Find the equation of l_2 , in terms of k .



- (c) Find the value of k for which l_2 passes through the point $Q(3, 11)$.



- (d) Hence, or otherwise, find the co-ordinates of the foot of the perpendicular from Q to l_1 .

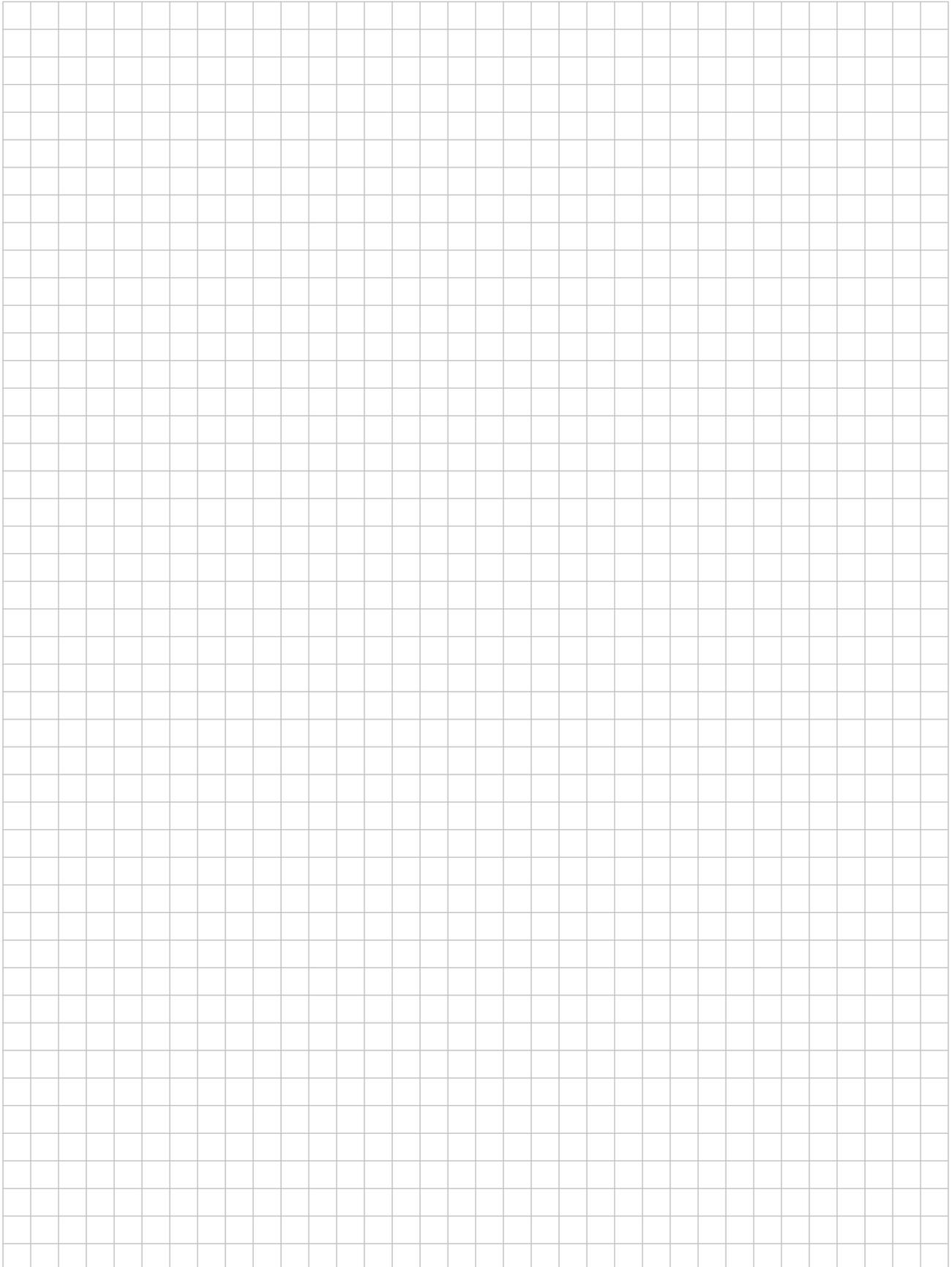


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Question 4

(25 marks)

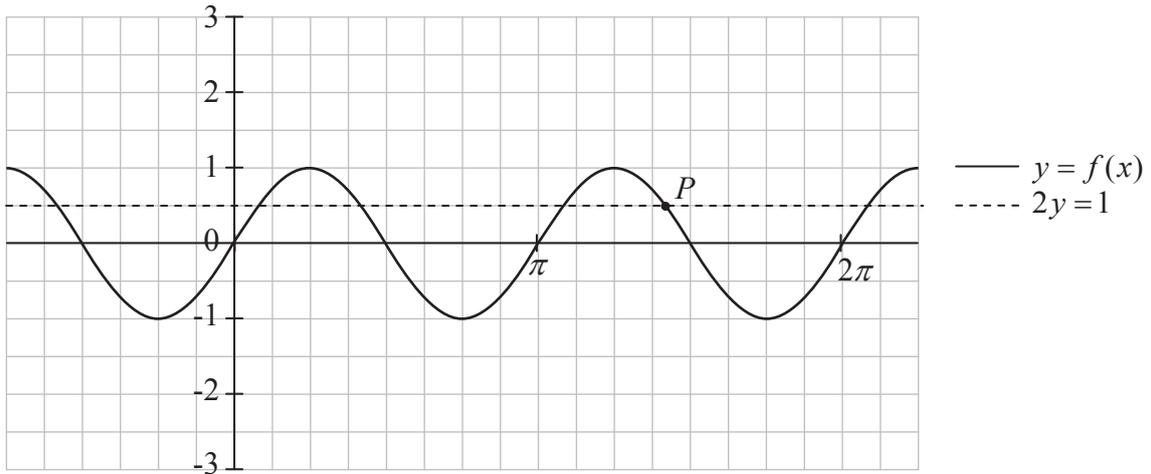
The centre of a circle lies on the line $x + 2y - 6 = 0$. The x -axis and the y -axis are tangents to the circle. There are two circles that satisfy these conditions. Find their equations.



Question 5

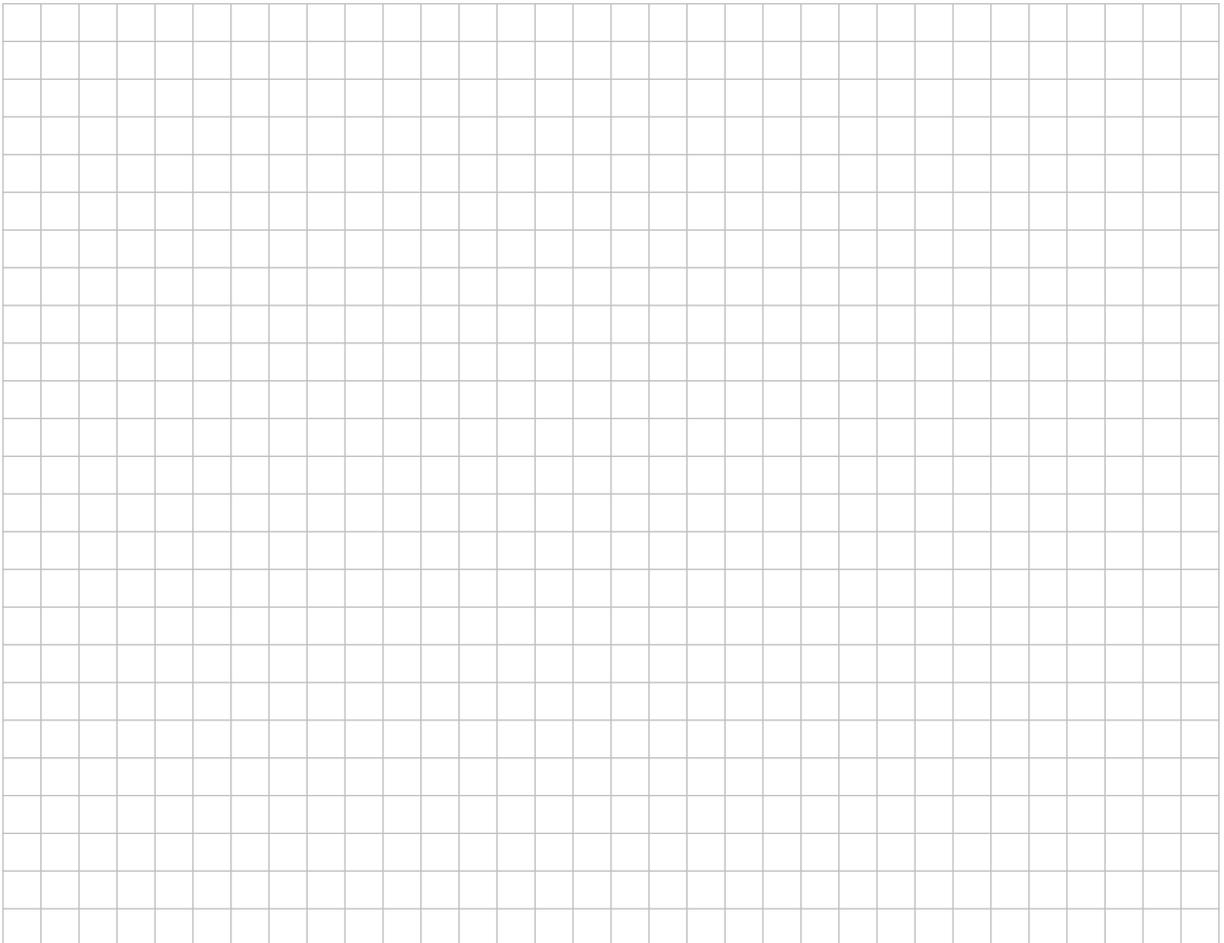
(25 marks)

The diagram below shows the graph of the function $f : x \mapsto \sin 2x$. The line $2y = 1$ is also shown.



(a) On the same diagram above, sketch the graphs of $g : x \mapsto \sin x$ and $h : x \mapsto 3 \sin 2x$. Indicate clearly which is g and which is h .

(b) Find the co-ordinates of the point P in the diagram.



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OR

Question 6B

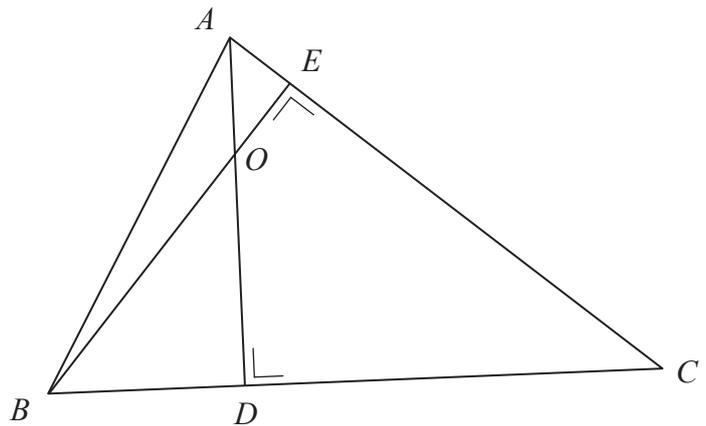
ABC is a triangle.

D is the point on BC such that $AD \perp BC$.

E is the point on AC such that $BE \perp AC$.

AD and BE intersect at O .

Prove that $|\angle DOC| = |\angle DEC|$.



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Answer Question 7, Question 8, and Question 9.

Question 7

(75 marks)

The *King of the Hill* triathlon race in Kinsale consists of a 750 metre swim, followed by a 20 kilometre cycle, followed by a 5 kilometre run.

The questions below are based on data from 224 athletes who completed this triathlon in 2010.

Máire is analysing data from the race, using statistical software. She has a data file with each competitor's time for each part of the race, along with various other details of the competitors.

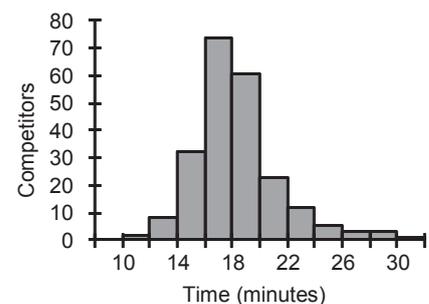
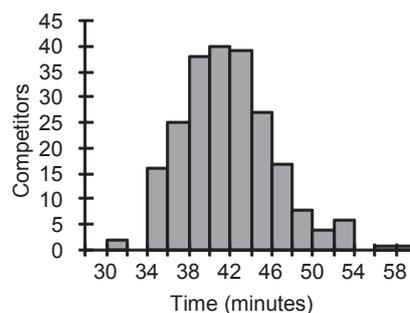
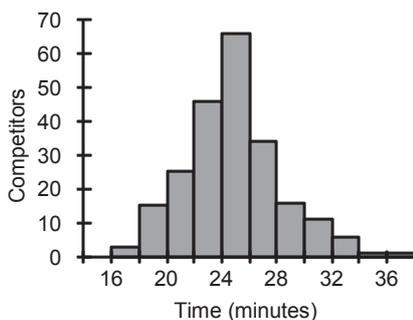


Lizzie Lee, winner of the women's event

Máire gets the software to produce some *summary statistics* and it produces the following table. Three of the entries in the table have been removed and replaced with question marks (?).

	Swim	Cycle	Run
Mean	18.329	41.927	?
Median	17.900	41.306	?
Mode	#N/A	#N/A	#N/A
Standard Deviation	?	4.553	3.409
Sample Variance	10.017	20.729	11.622
Skewness	1.094	0.717	0.463
Range	19.226	27.282	20.870
Minimum	11.350	31.566	16.466
Maximum	30.576	58.847	37.336
Count	224	224	224

Máire produces histograms of the times for the three events. Here are the three histograms, without their titles.



Question 8

(50 marks)

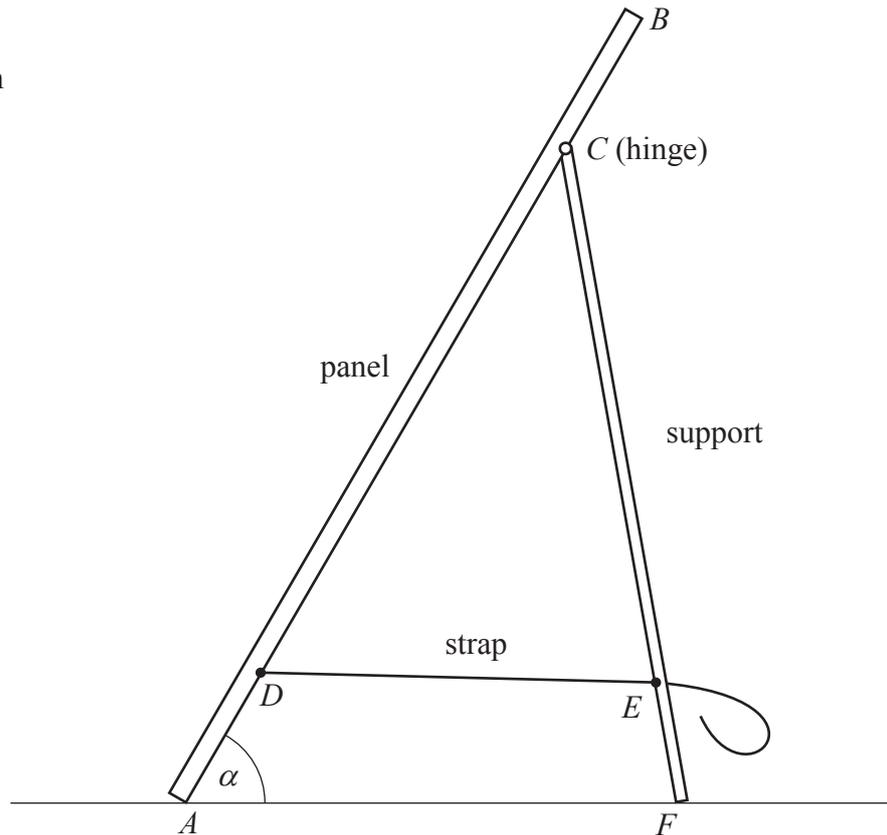
A stand is being used to prop up a portable solar panel. It consists of a support that is hinged to the panel near the top, and an adjustable strap joining the panel to the support near the bottom.



By adjusting the length of the strap, the angle between the panel and the ground can be changed.

The dimensions are as follows:

- $|AB| = 30$ cm
- $|AD| = |CB| = 5$ cm
- $|CF| = 22$ cm
- $|EF| = 4$ cm.



- (a) Find the length of the strap $[DE]$ such that the angle α between the panel and the ground is 60° .

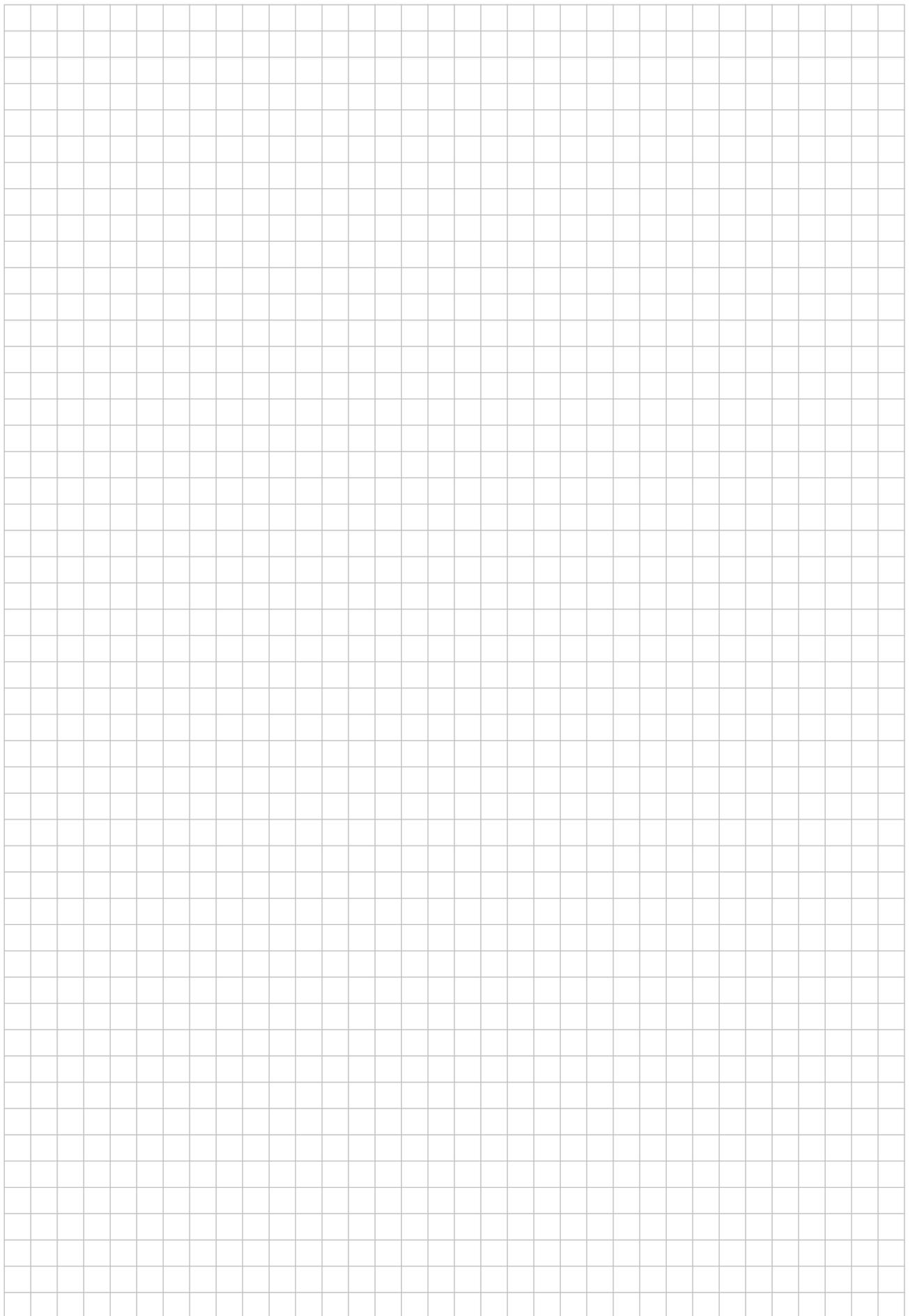


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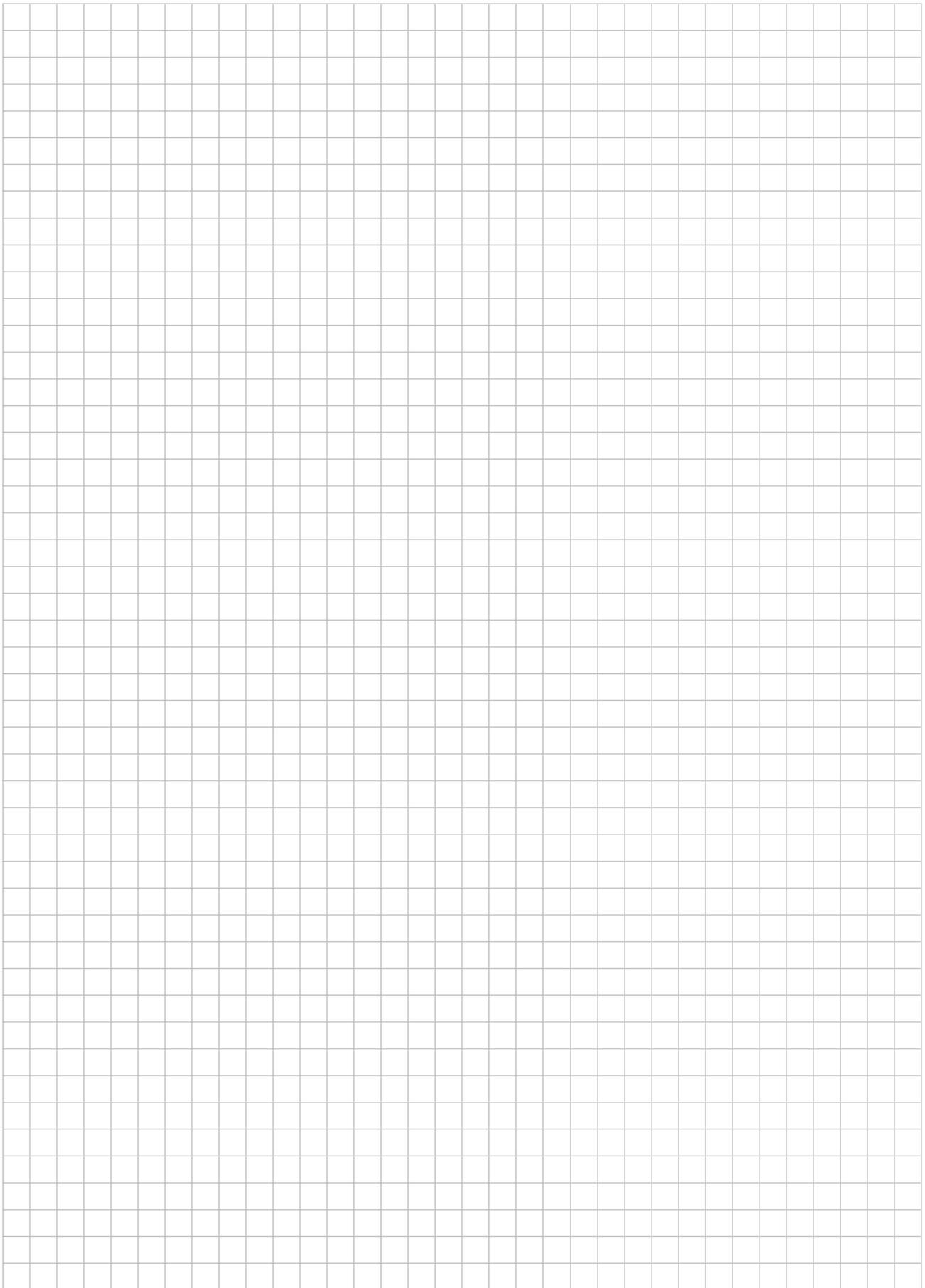


(b) Find the maximum possible value of α , correct to the nearest degree.



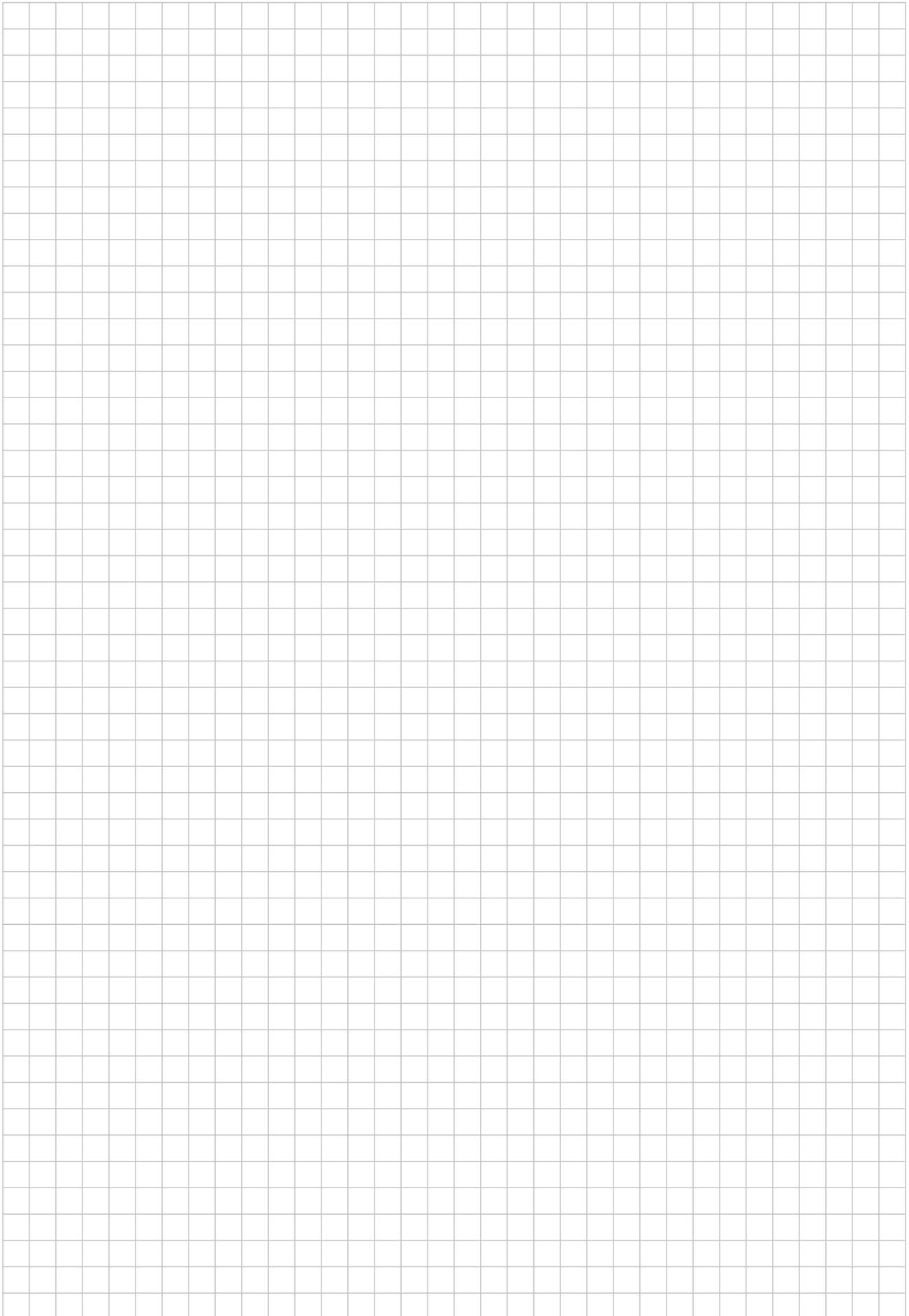


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Note to readers of this document:

This sample paper is intended to help teachers and candidates prepare for the June 2013 examination in *Mathematics* under Phase 2 of *Project Maths*. The content and structure do not necessarily reflect the 2014 or subsequent examinations.

Section A of the examination paper will consist of six questions, each carrying 25 marks. In accordance with the footnote in the syllabus in relation to geometry, there will be a choice within Question 6, as illustrated here.

Section B will consist of two, three, or four questions. These questions will not necessarily carry equal marks. The number of marks for each will be stated on the examination paper. The total number of marks for Section B will be 150.

Leaving Certificate 2013 – Higher Level

Mathematics (Project Maths – Phase 2) – Paper 2

Sample Paper

Time: 2 hours 30 minutes