

Instructions

There are **two** sections in this examination paper.

Section A	Concepts and Skills	150 marks	6 questions
Section B	Contexts and Applications	150 marks	2 questions

Answer **all eight** questions, as follows:

In Section A, answer:

Questions 1 to 5 and

either Question 6A **or** Question 6B.

In Section B, answer Question 7 and Question 8.

Write your answers in the spaces provided in this booklet. There is space for extra work at the back of the booklet. You may also ask the superintendent for more paper. Label any extra work clearly with the question number and part.

The superintendent will give you a copy of the booklet of *Formulae and Tables*. You must return it at the end of the examination. You are not allowed to bring your own copy into the examination.

Marks will be lost if all necessary work is not clearly shown.

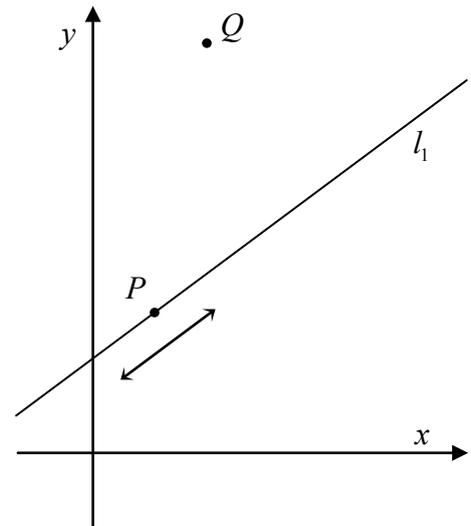
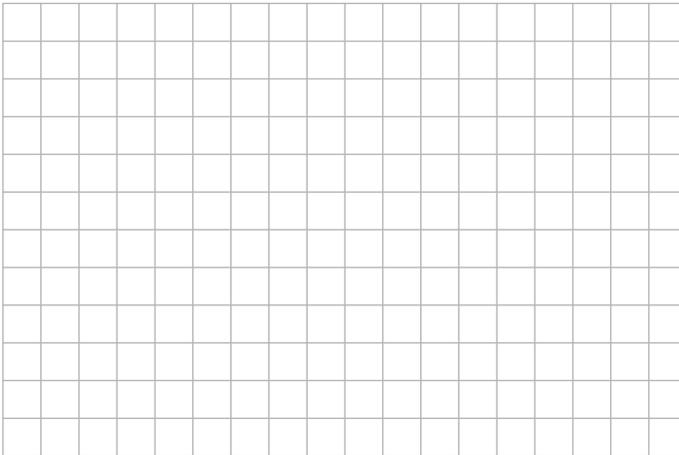
Answers should include the appropriate units of measurement, where relevant.

Answers should be given in simplest form, where relevant.

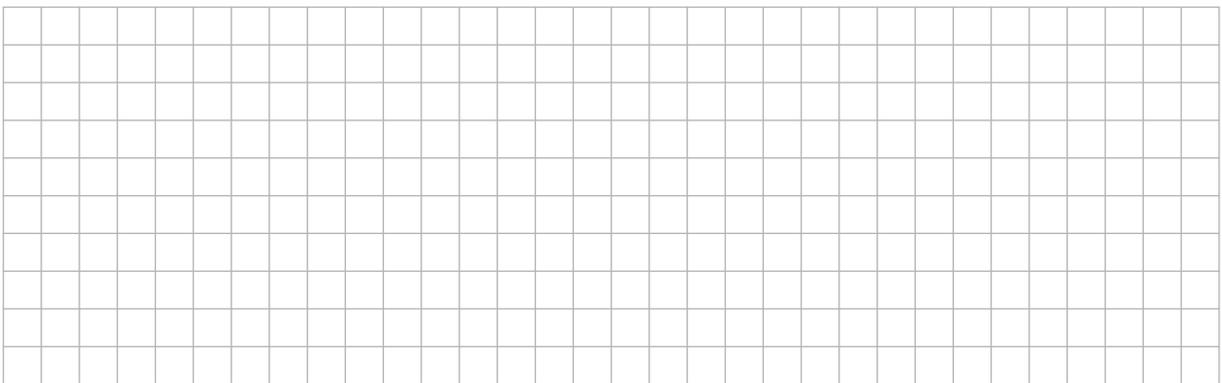
Question 3

(25 marks)

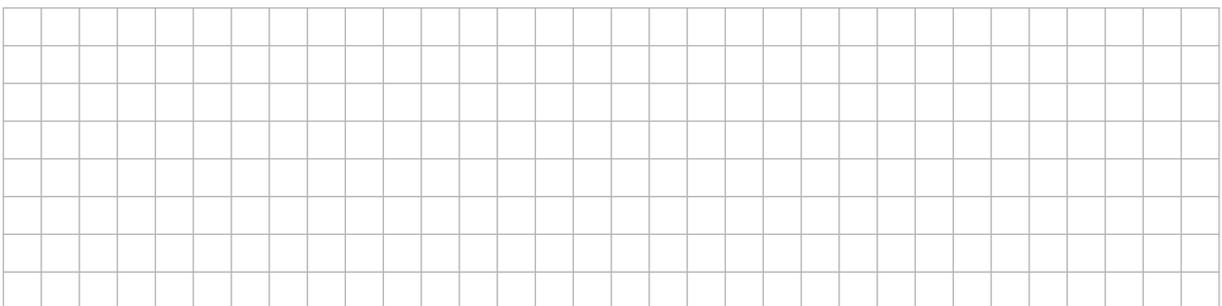
- (a) Show that, for all $k \in \mathbb{R}$, the point $P(4k - 2, 3k + 1)$ lies on the line $l_1 : 3x - 4y + 10 = 0$.



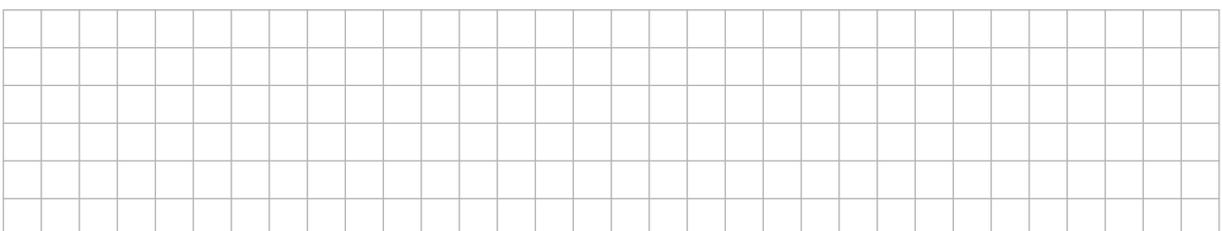
- (b) The line l_2 passes through P and is perpendicular to l_1 . Find the equation of l_2 , in terms of k .



- (c) Find the value of k for which l_2 passes through the point $Q(3, 11)$.



- (d) Hence, or otherwise, find the co-ordinates of the foot of the perpendicular from Q to l_1 .

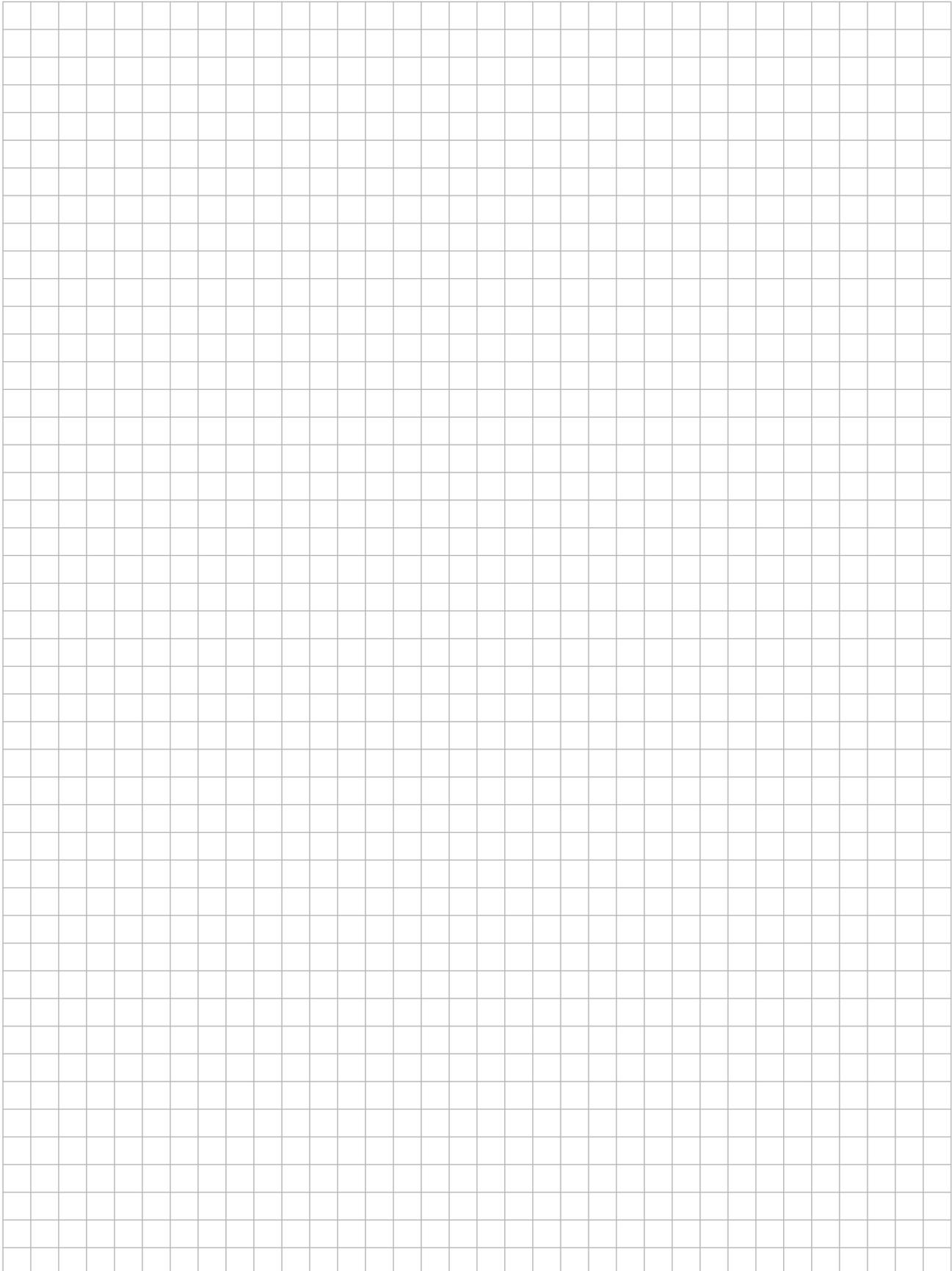


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Question 4

(25 marks)

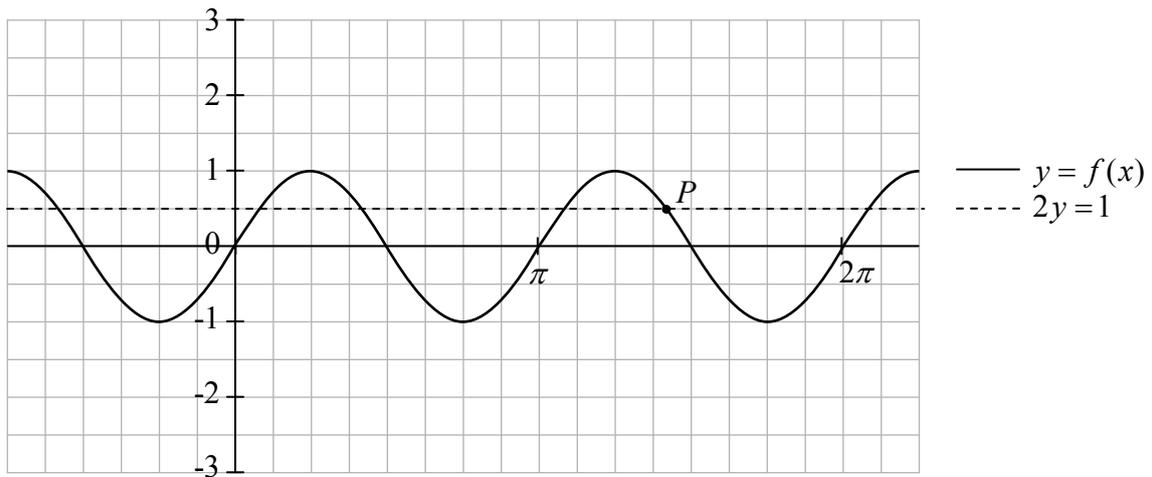
The centre of a circle lies on the line $x + 2y - 6 = 0$. The x -axis and the y -axis are tangents to the circle. There are two circles that satisfy these conditions. Find their equations.



Question 5

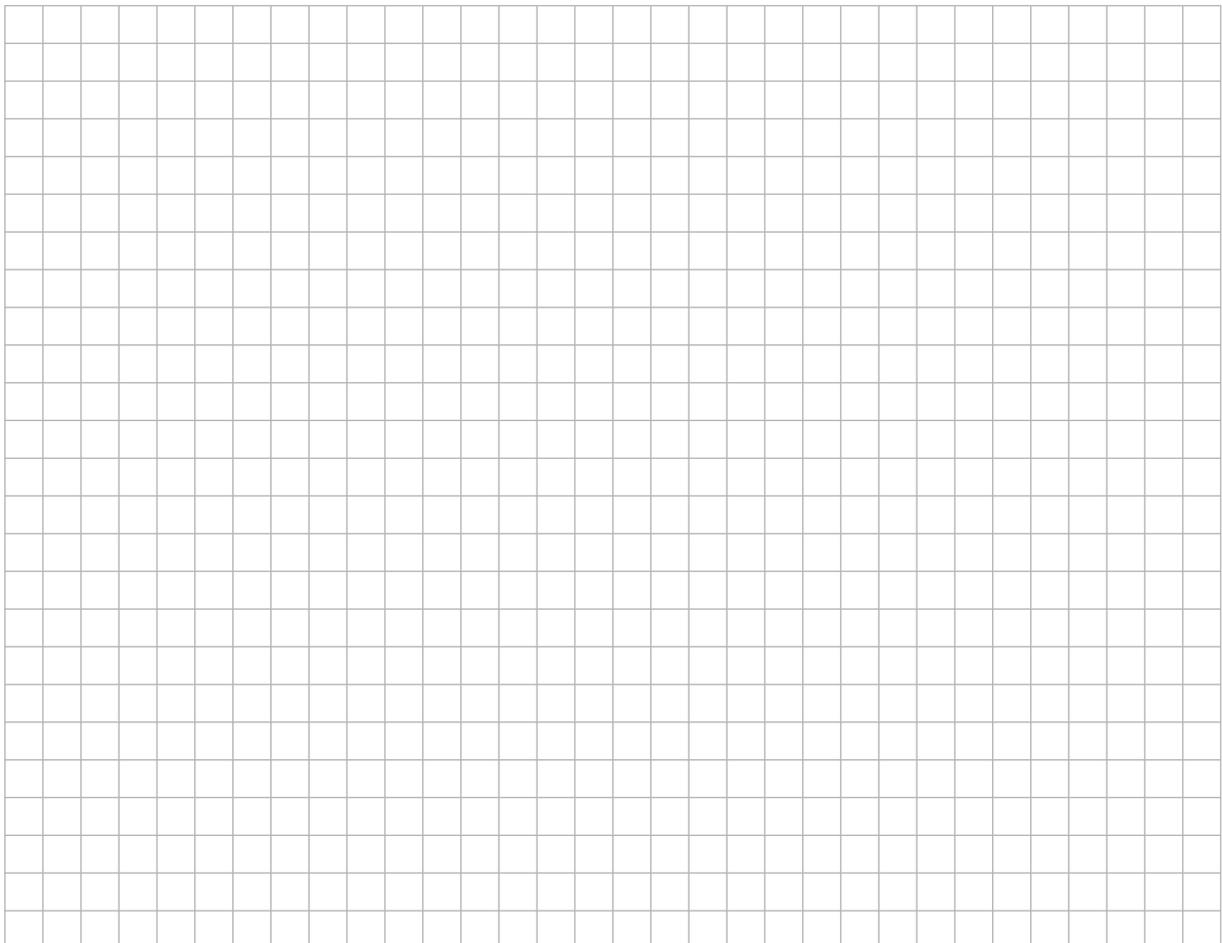
(25 marks)

The diagram below shows the graph of the function $f : x \mapsto \sin 2x$. The line $2y = 1$ is also shown.



(a) On the same diagram above, sketch the graphs of $g : x \mapsto \sin x$ and $h : x \mapsto 3 \sin 2x$. Indicate clearly which is g and which is h .

(b) Find the co-ordinates of the point P in the diagram.



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Answer Question 7 and Question 8.

Question 7

(75 marks)

The *King of the Hill* triathlon race in Kinsale consists of a 750 metre swim, followed by a 20 kilometre cycle, followed by a 5 kilometre run.

The questions below are based on data from 224 athletes who completed this triathlon in 2010.

Máire is analysing data from the race, using statistical software. She has a data file with each competitor's time for each part of the race, along with various other details of the competitors.

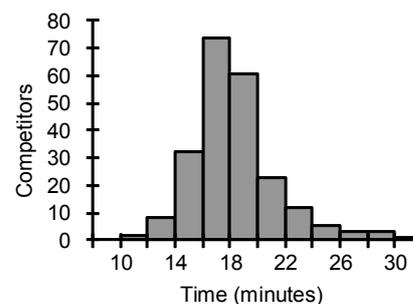
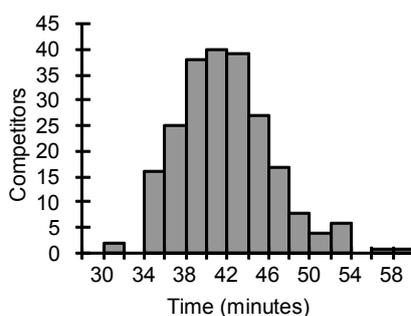
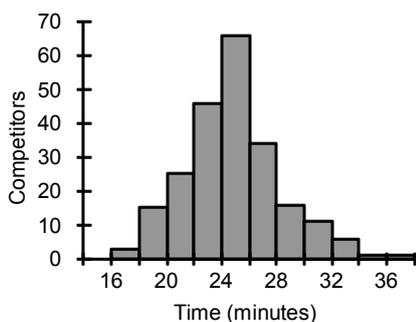


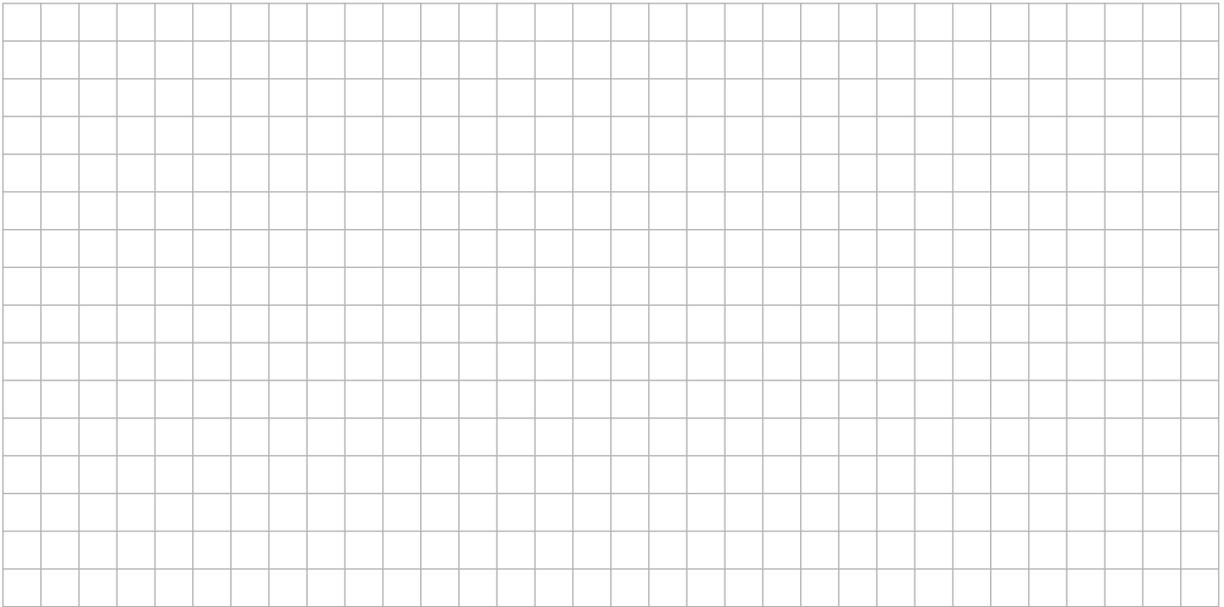
Lizzie Lee, winner of the women's event

Máire gets the software to produce some *summary statistics* and it produces the following table. Three of the entries in the table have been removed and replaced with question marks (?).

	Swim	Cycle	Run
Mean	18.329	41.927	?
Median	17.900	41.306	?
Mode	#N/A	#N/A	#N/A
Standard Deviation	?	4.553	3.409
Sample Variance	10.017	20.729	11.622
Skewness	1.094	0.717	0.463
Range	19.226	27.282	20.870
Minimum	11.350	31.566	16.466
Maximum	30.576	58.847	37.336
Count	224	224	224

Máire produces histograms of the times for the three events. Here are the three histograms, without their titles.





(ii) Find the maximum possible value of α , correct to the nearest degree.

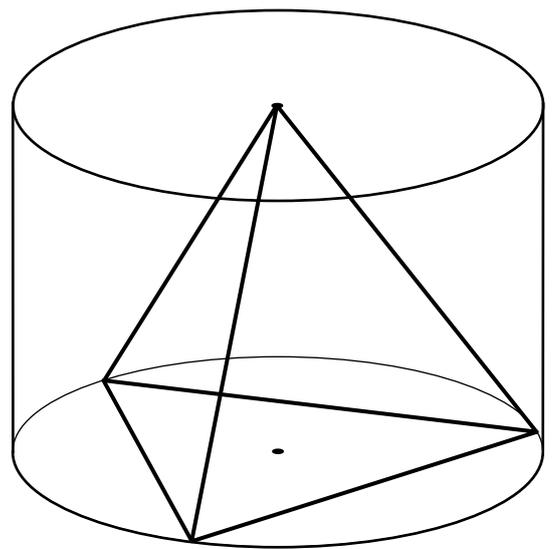


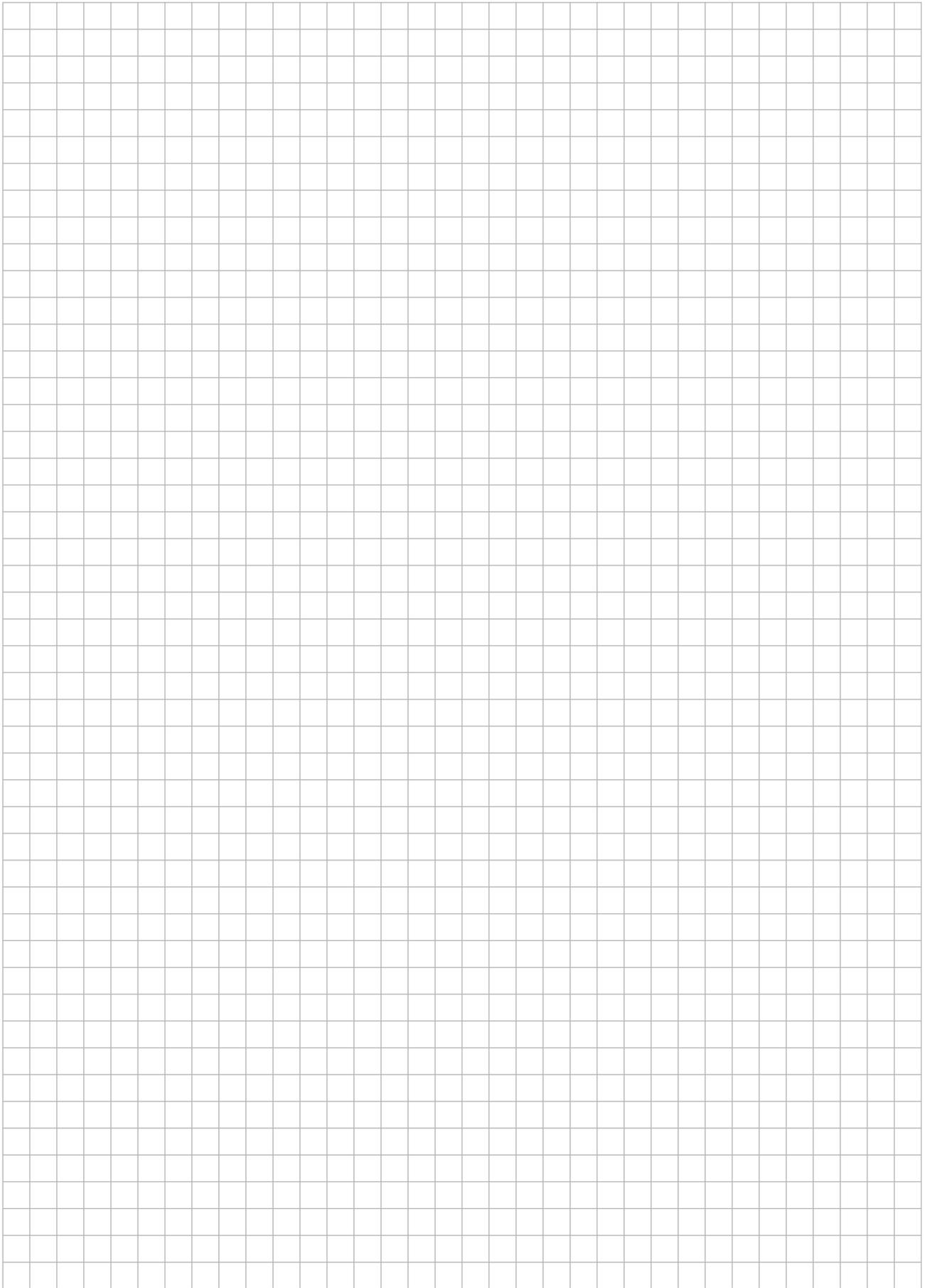
(b) A regular tetrahedron has four faces, each of which is an equilateral triangle.

A wooden puzzle consists of several pieces that can be assembled to make a regular tetrahedron. The manufacturer wants to package the assembled tetrahedron in a clear cylindrical container, with one face flat against the bottom.

If the length of one edge of the tetrahedron is $2a$, show that the volume of the smallest

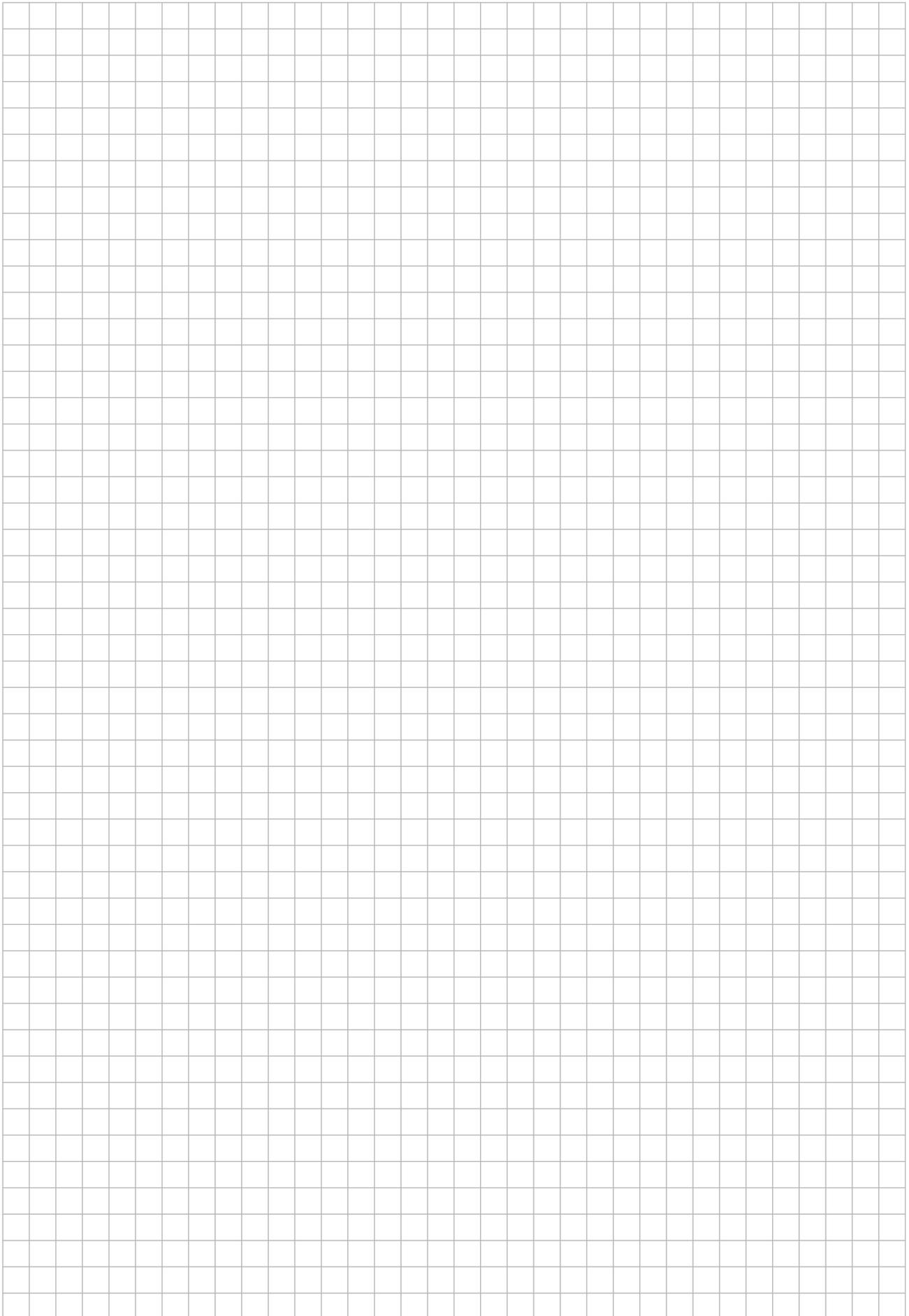
possible cylindrical container is $\left(\frac{8\sqrt{6}}{9}\right)\pi a^3$.



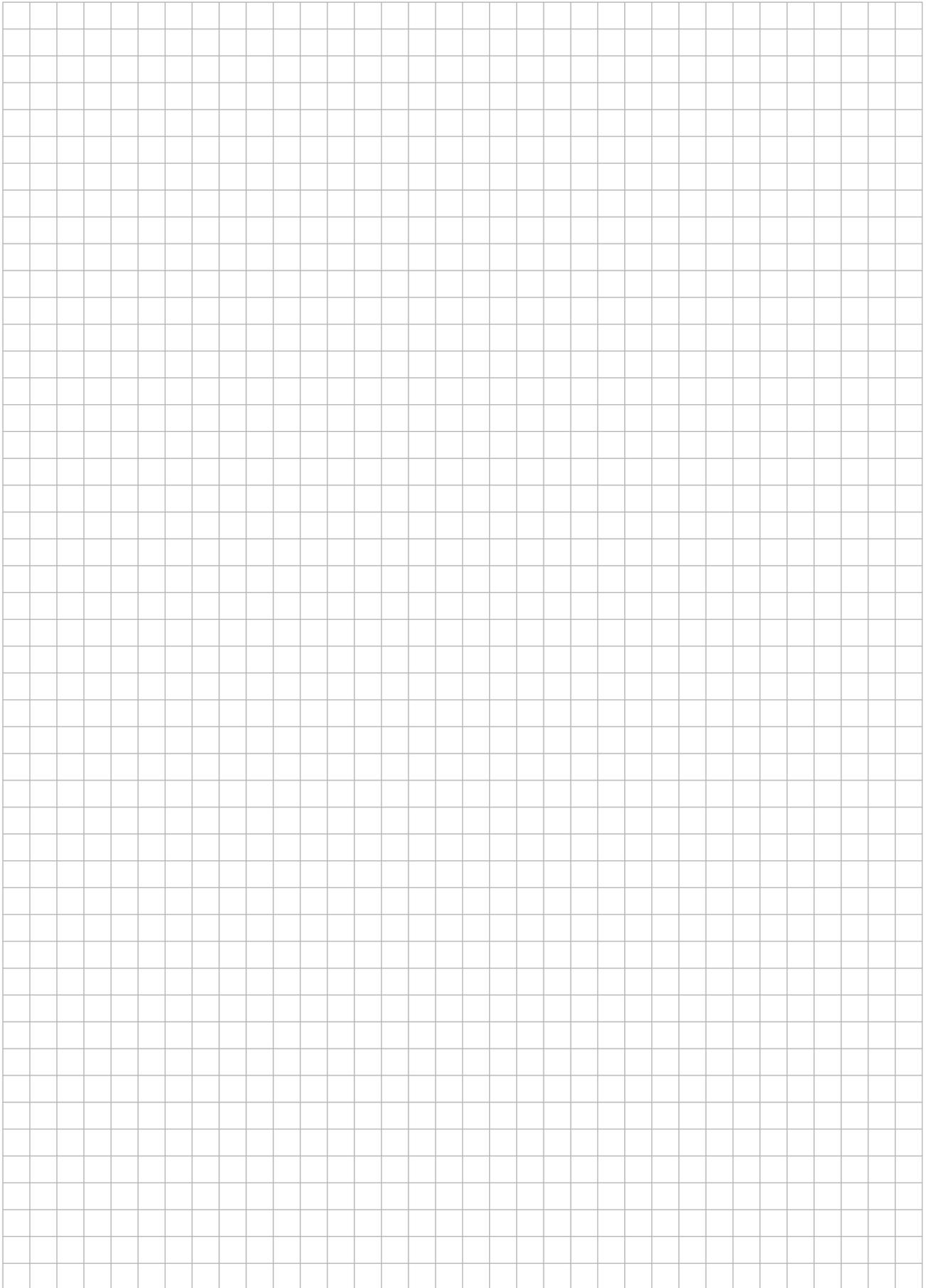


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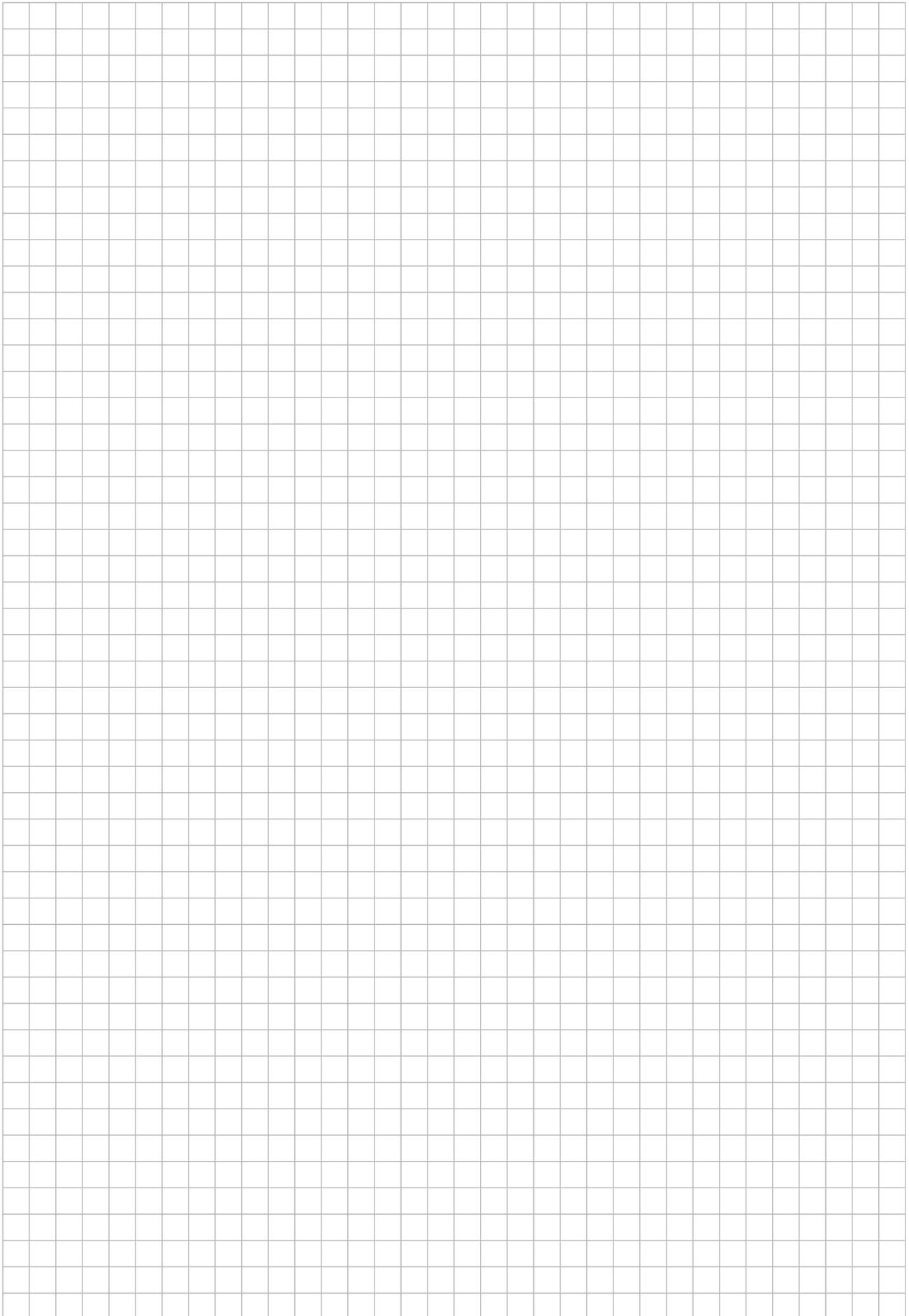


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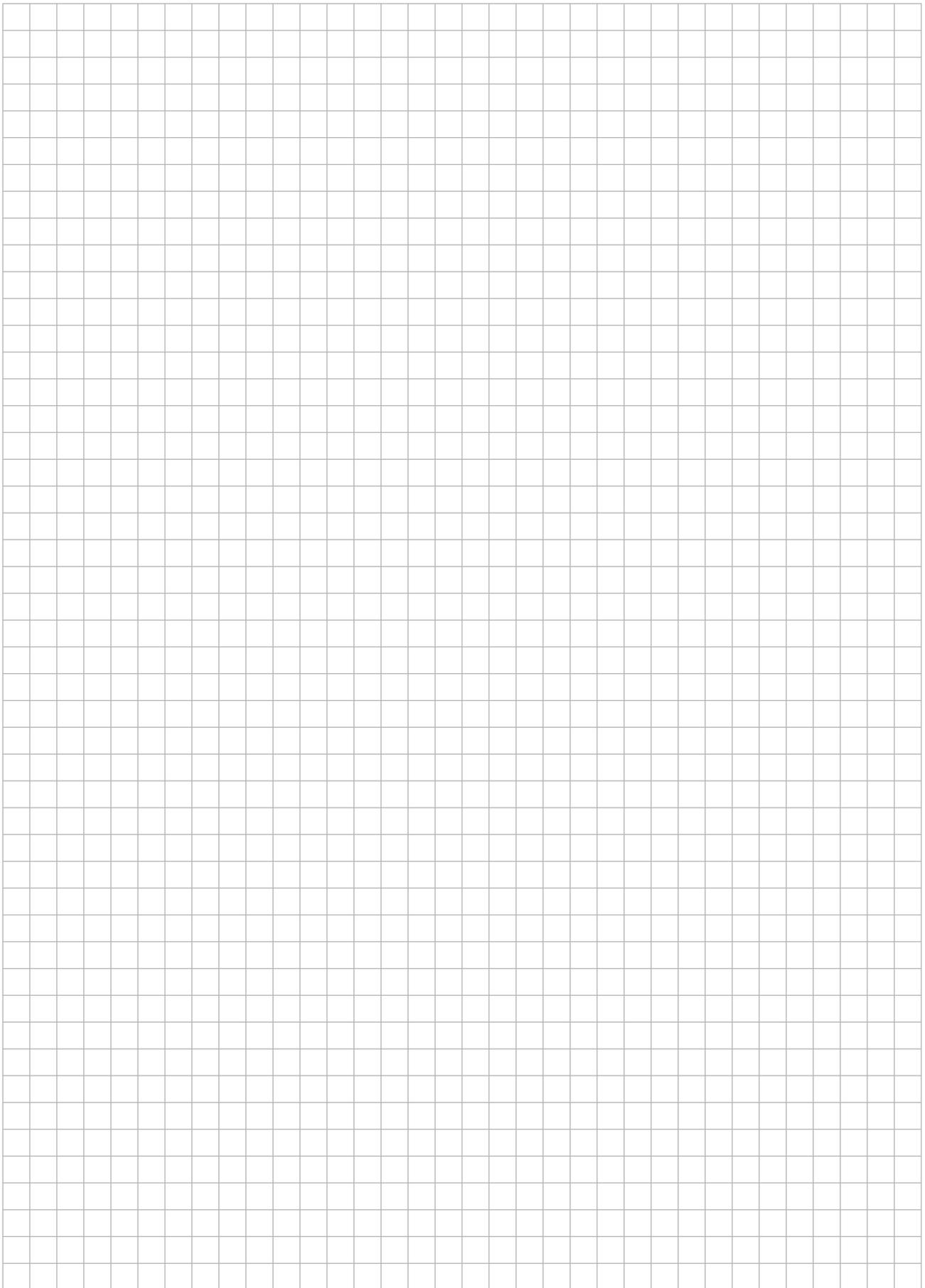


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Note to readers of this document:

This sample paper is intended to help teachers and candidates prepare for the June 2011 examination in the *Project Maths* initial schools. The content and structure do not necessarily reflect the 2012 or subsequent examinations in the initial schools or in all other schools.

Leaving Certificate 2011 – Higher Level

Mathematics (Project Maths – Phase 2) – Paper 2

Sample Paper

Time: 2 hours 30 minutes