

# Coimisiún na Scrúduithe Stáit 

 State Examinations CommissionJUNIOR CERTIFICATE EXAMINATION, 2004

## MATHEMATICS - ORDINARY LEVEL - PAPER 1 (300 marks)

THURSDAY, JUNE 10 - MORNING, 9:30 to 11:30
Time: 2 hours

Attempt ALL questions. Each question carries 50 marks.

Answers and supporting work should be written into the boxes provided.
Extra paper and graph paper can be obtained from the Superintendent, if needed.
The symbol indicates that supporting work must be shown to obtain full marks.

Make and model of calculator used:
$\square$
For Superintendent/Examiner use only:
Centre Stamp


| Question | Mark |
| :---: | :---: |
| $\mathbf{1}$ |  |
| $\mathbf{2}$ |  |
| $\mathbf{3}$ |  |
| $\mathbf{4}$ |  |
| $\mathbf{5}$ |  |
| $\mathbf{6}$ |  |
| Total |  |
| Grade |  |

1. (a) (i) Using the Venn diagram below, shade in the region that represents $P \cap Q$.

(ii) Using the Venn diagram below, shade in the region that represents $P \cup Q$.

(1(b) $U$ is the universal set.
$A=\{3,8,9\}$
$B=\{1,2,6,8,9\}$
$C=\{1,2,4,5,8\}$


List the elements of:
(i) $A \cup B$
(ii) $B \backslash C$
(iii) $A^{\prime}$
(iv) $A \cup(B \backslash C)$
(c) (i) $\quad \mathrm{P}$ is the set of prime numbers between 1 and 12.

List the elements of the set $P$.

(ii) $\mathrm{Q}=\{1,3,5,7,9,11\}$.

Write down \# Q.
$\square$
(iii) $\mathrm{T}=\{2,4,6,8,10,12\}$.

Write down the elements of T that are multiples of 3 .
(iv) Express 12 as the product of three prime numbers.
2. (a) $€ 400$ is shared between Mary and Tom in the ratio 7:3.

How much does each receive?


2(b) (i) Simplify $\frac{a^{7} \times a^{4}}{a^{3} \times a^{2}}$, giving your answer in the form $a^{n}$, where $n \in \mathbf{N}$.
$\square$
(ii) By rounding each of these numbers to the nearest whole number, estimate the value of $\frac{66 \cdot 88-27 \cdot 36}{7 \cdot 6}$.
$\frac{66 \cdot 88-27 \cdot 36}{7 \cdot 6}$ is approximately equal to:

(iii) Using a calculator, or otherwise, find the exact value of $\frac{66 \cdot 88-27 \cdot 36}{7 \cdot 6}$.
$\square$

2(c) Using a calculator, or otherwise, find the exact value of:
(i) $9^{\frac{1}{2}}$
(ii) $(5 \cdot 32)^{2}$
(iii) Hence, evaluate $9^{\frac{1}{2}}+(5 \cdot 32)^{2} \times \frac{1}{0.625}$ and give your answer correct to two decimal places.

3. (a) Anne bought 2 cans of cola. Each can cost 80 c.

How much change did she get from a $€ 10$ note?


3(b) (i) John's gross pay is $€ 21000$. His tax credit is $€ 2369$. He pays income tax at the rate of $22 \%$.
What is his take-home pay?

|  |  |  |  |
| :--- | :--- | :---: | :---: |
| $\qquad$Gross Pay $€ 21000$ <br> Tax @ 22\%  <br> Tax Credit $€ 2369$ <br> Tax Due  <br> Take-home Pay  |  |  |  |

(ii) VAT at $15 \%$ is added to a bill of $€ 84 \cdot 60$.

Calculate the total bill.

3(c) (i) $€ 3000$ is invested at $4 \%$ per annum.
What is the amount of the investment at the end of one year?

(ii) $€ 500$ is withdrawn from this amount at the beginning of the second year.

The interest rate for the second year is $3 \cdot 6 \%$ per annum.
What is the amount of the investment at the end of that year?
$\square$
4. (a) If $a=2$ and $b=7$, find the value of :
$\square$

4(b) (i) Solve the equation

$$
5(2 x+1)=45 .
$$

$\square$
(ii) Write in its simplest form

$$
(6 x-y)-3(x-2 y+1)
$$

4(c) The cost of five books and one magazine is $€ 32$.
The cost of eight books and three magazines is $€ 54$.
Let $€ x$ be the cost of a book and let $€ y$ be the cost of a magazine.
(i) Write down two equations, each in $x$ and $y$, to represent the above information.

First equation:

Second equation:
(ii) Solve these equations to find the cost of a book and the cost of a magazine.
$\square$
5. (a) Find the values of $x$ for which

$$
2 x+1 \leq 7, x \in \mathbf{N} .
$$

## 2

5(b) (i) Factorise $3 x-3 y+a x-a y$.

$$
3 x-3 y+a x-a y
$$

(ii) Factorise $\quad x^{2}-25$.

$$
x^{2}-25
$$

(iii) Express $\frac{2}{3}-\frac{1}{9}$ as a single fraction.

$$
\frac{2}{3}-\frac{1}{9}=
$$

(iv) Express $\frac{x+7}{3}-\frac{x}{9}$ as a single fraction.

Give your answer in its simplest form.
2 $\frac{x+7}{3}-\frac{x}{9}=$

5(c) (i) Solve the equation $x^{2}-3 x-10=0$.

(ii) Multiply $(x-4)$ by $\left(x^{2}+3 x-1\right)$.

Give your answer in its simplest form.

6. (a) $\mathrm{P}=\{(1,5),(2,5),(3,6),(4,6)\}$.

Write out the domain and range of $P$.

Domain $=$

Range $=$

6(b) Draw the graph of the function

$$
f: x \rightarrow x^{2}-4 x+2
$$

in the domain $0 \leq x \leq 4$, where $x \in \mathbf{R}$.
$\square$

|  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

6(c) (i) Draw the axis of symmetry of the graph drawn in 6 (b) above. Work to be shown on the graph.
(ii) Use the graph to estimate the values of $x$ for which $f(x)=0$.

Work to be shown on the graph and answers to be written here.

Space for extra work


