



Coimisiún na Scrúduithe Stáit
State Examinations Commission

Junior Certificate Examination 2015

Mathematics

Paper 1
Higher Level

Friday 5 June – Afternoon 2:00 to 4:30

300 marks

Examination number

Centre Stamp

Running total	
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For examiner			
Question	Mark	Question	Mark
1		11	
2		12	
3		13	
4		14	
5			
6			
7			
8			
9			
10		Total	

Grade

Instructions

There are 14 questions on this examination paper. Answer **all** questions.

Questions do not necessarily carry equal marks. To help you manage your time during this examination, a maximum time for each question is suggested. If you remain within these times you should have about 10 minutes left to review your work.

Write your answers in the spaces provided in this booklet. You may lose marks if you do not do so. You may ask the superintendent for more paper. Label any extra work clearly with the question number and part.

The superintendent will give you a copy of the *Formulae and Tables* booklet. You must return it at the end of the examination. You are not allowed to bring your own copy into the examination.

You will lose marks if all necessary work is not clearly shown.

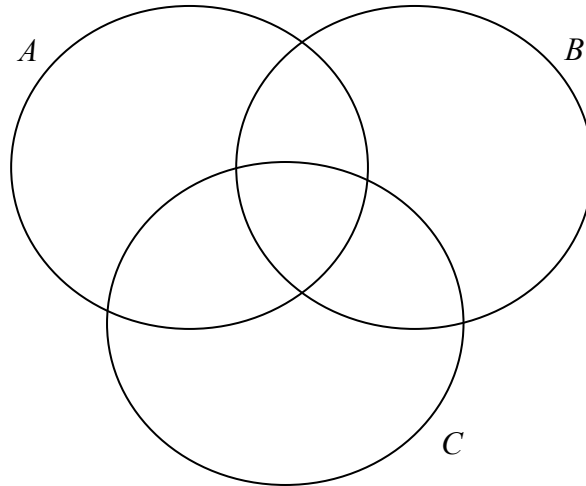
You may lose marks if the appropriate units of measurement are not included, where relevant.

You may lose marks if your answers are not given in simplest form, where relevant.

Write the make and model of your calculator(s) here:

Question 1**(Suggested maximum time: 10 minutes)**The sets A , B , and C are as follows:

$$A = \{1, 2, 3, 5, 6, 7\} \quad B = \{2, 3, 4, 5, 8, 9\} \quad C = \{1, 4, 5, 10\}.$$

(a) Complete the Venn diagram below.**(b)** List the elements of each of the following sets.

$$A \cup B = \underline{\hspace{10cm}}$$

$$A \setminus C = \underline{\hspace{10cm}}$$

$$A \cup (B \cap C) = \underline{\hspace{10cm}}$$

(c) Complete the following identity.

$$A \cup (B \cap C) = (A \cup B) \cap (\underline{\hspace{2cm}})$$

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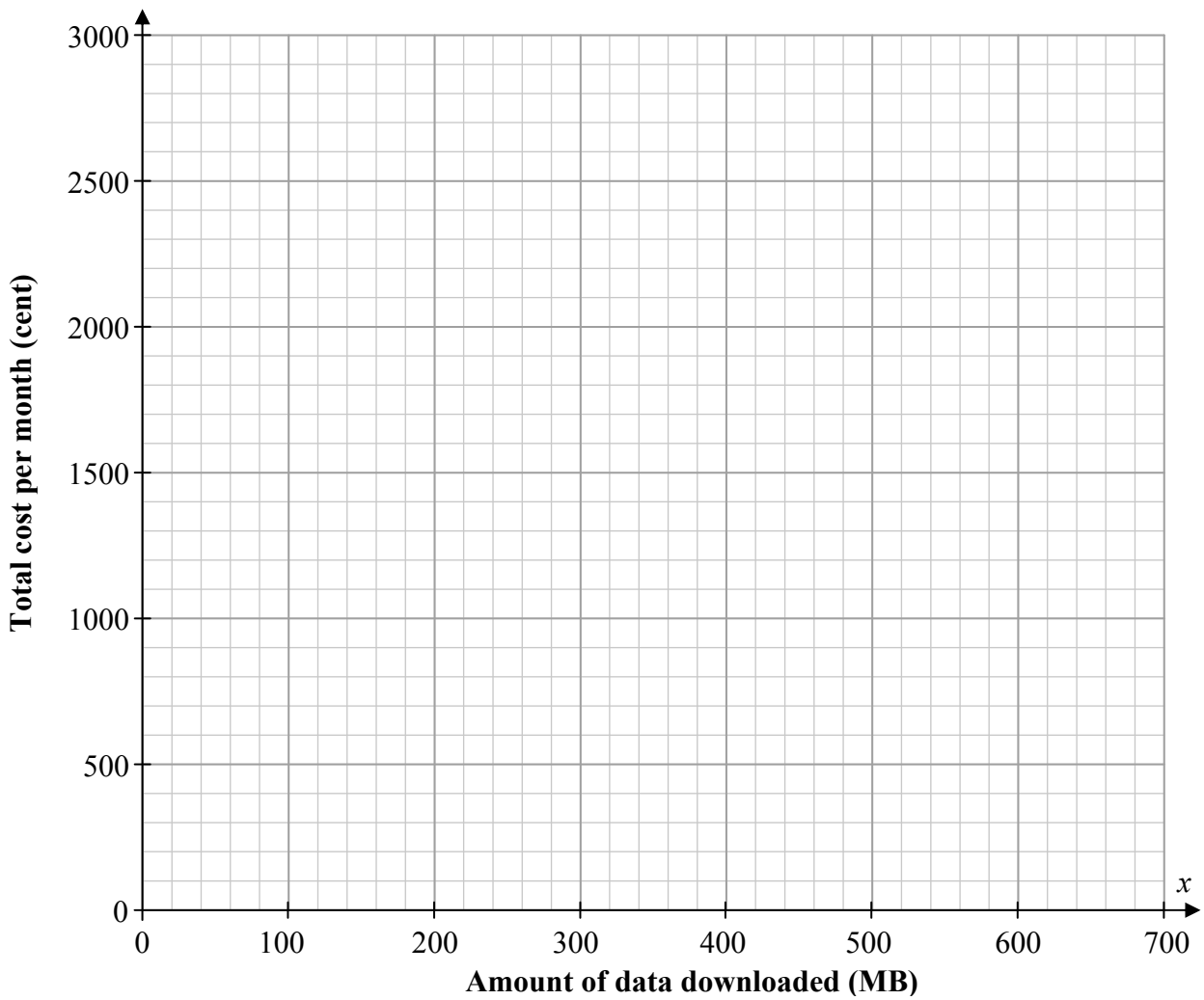
Question 6

(Suggested maximum time: 15 minutes)

Two mobile phone companies, *Cellulon* and *Mobil*, offer price plans for mobile internet access. A formula, in x , for the total cost per month for each company is shown in the table below. x is the number of MB of data downloaded per month.

Phone company	Total cost per month (cent)
<i>Cellulon</i>	$c(x) = 4x$
<i>Mobil</i>	$m(x) = 1000 + 2x$

- (a) Draw the graphs of $c(x)$ and $m(x)$ on the co-ordinate grid below to show the total cost per month for each phone company, for $0 \leq x \leq 700$. Label each graph clearly.



- (b) Which company charges **no** fixed monthly fee?
Justify your answer, with reference to the relevant **formula** or **graph**.

Answer:																						
Reason:																						

- (c) Write down the **point of intersection** of the two graphs.

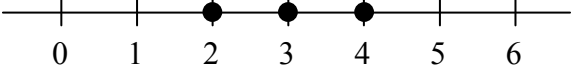
Fergus wants to buy a mobile phone from one of these two companies, and wants his mobile internet bill to be as low as possible.

- (d) **Explain** how your answer to part (c) would help Fergus choose between *Cellulon* and *Mobil*.

Question 8

(Suggested maximum time: 5 minutes)

(a) Complete the inequality in n below so that it has the solution set shown.

Inequality	Solution Set
<div style="display: flex; align-items: center; justify-content: center;"><div style="border: 1px solid black; width: 60px; height: 30px; display: inline-block; margin-right: 10px;"></div>$\leq n \leq$<div style="border: 1px solid black; width: 60px; height: 30px; display: inline-block; margin-left: 10px;"></div>$, n \in \mathbb{N}.$</div>	 <p>A horizontal number line with tick marks at 0, 1, 2, 3, 4, 5, and 6. Solid black dots are placed at the positions of 2, 3, and 4.</p>

(b) Complete the inequality in x below so that there is only **one** possible value of x , where $x \in \mathbb{R}$.

$$\boxed{} \leq x \leq \boxed{}, \quad x \in \mathbb{R}.$$

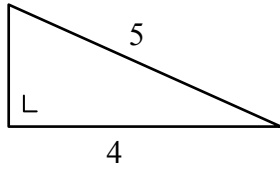
Question 11

(Suggested maximum time: 20 minutes)

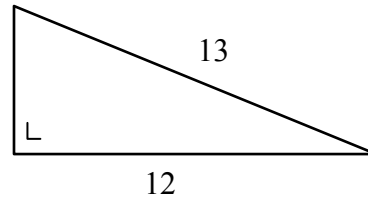
Two right-angled triangles are shown below.

- (a) Find the height of each triangle.

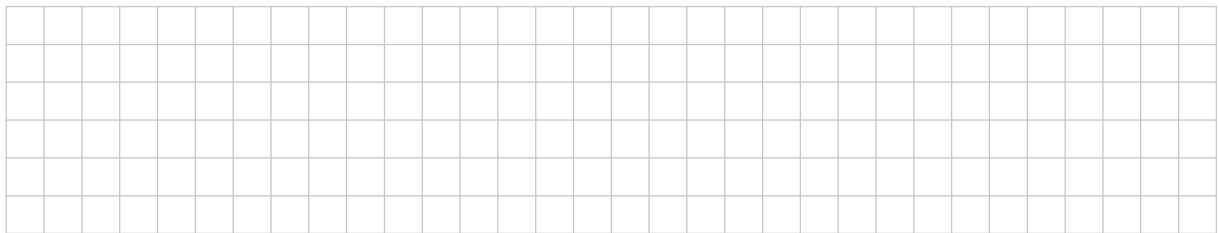
Write each answer in the box below the appropriate diagram.



Height =



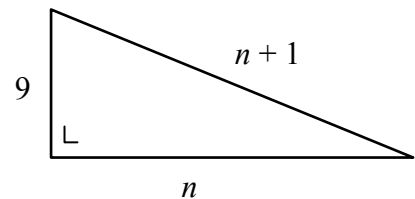
Height =



The triangles above are the first two triangles (with sides of integer lengths) where the hypotenuse is 1 unit longer than the base.

- (b) Another such triangle is shown on the right. It has a height of 9 units.

Use the Theorem of Pythagoras to find the value of n , the length of the base of this triangle.



Question 13

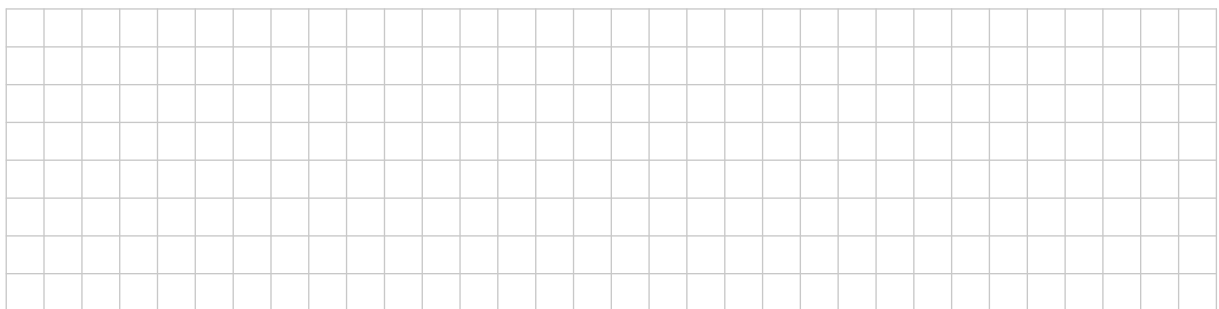
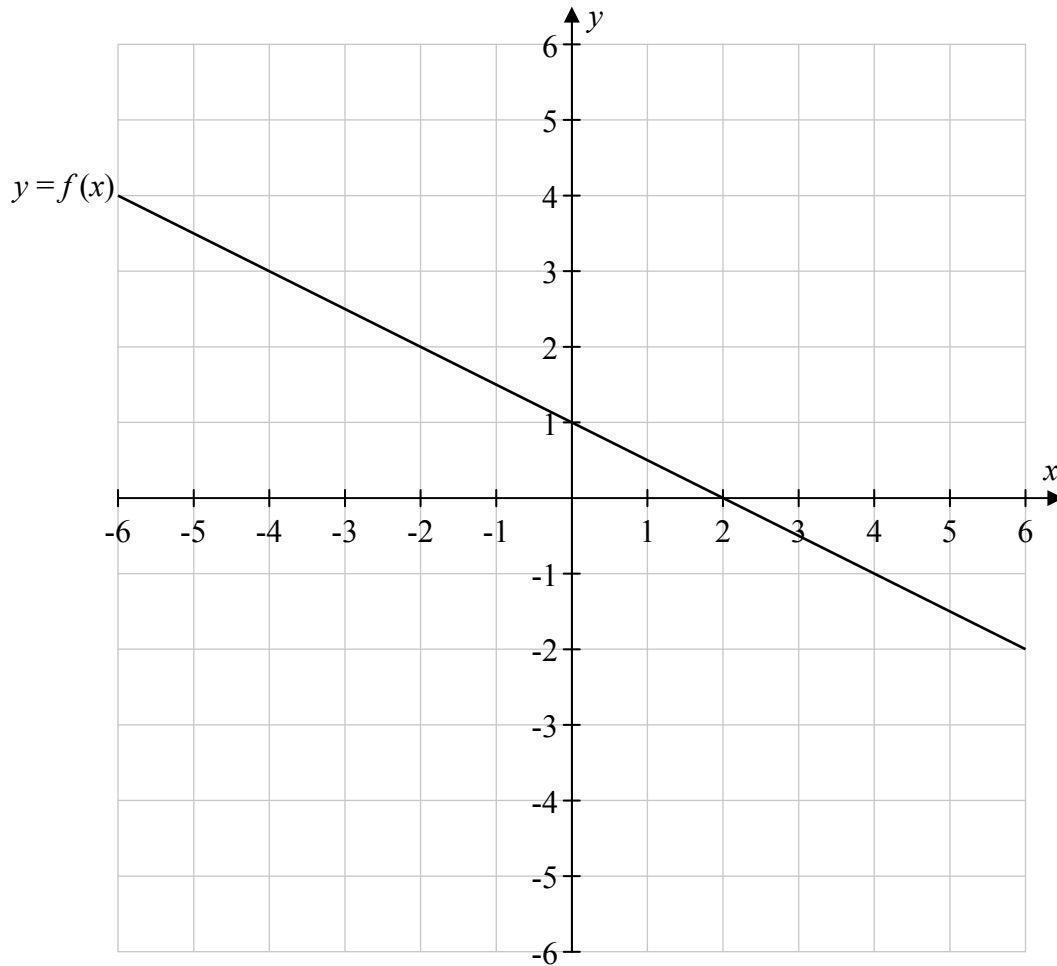
(Suggested maximum time: 5 minutes)

The graph of the linear function $y = f(x)$ is drawn on the co-ordinate grid below.

Using the same axes, draw the graph of each of the following functions, where $-6 \leq x \leq 6$, $x \in \mathbb{R}$.
Label each graph clearly.

(a) $y = f(x) + 2$

(b) $y = -f(x)$

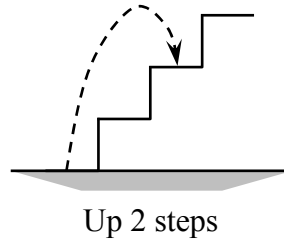
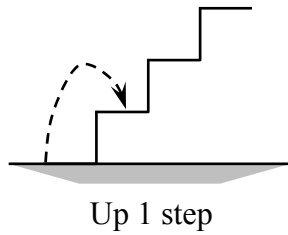


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Question 14

(Suggested maximum time: 20 minutes)

A boxer runs up stairs as part of her training.
She can go up 1 step or 2 steps with each stride, as shown.



The boxer wants to count how many different ways she can reach the n th step.
She calls this T_n , the n th Taylor number.

For example, she has 3 different ways to reach the 3rd step, as shown in the tables below.
So $T_3 = 3$.

3rd step: way 1
Up 1 step, then 1 step, then 1 step
$1 + 1 + 1$

3rd step: way 2
Up 1 step, then 2 steps
$1 + 2$

3rd step: way 3
Up 2 steps, then 1 step
$2 + 1$

(a) Find the value of T_1 and T_2 .

$T_1 = \underline{\hspace{2cm}}$	$T_2 = \underline{\hspace{2cm}}$
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(b) List all the different ways that she can reach the 4th step; one way is already done for you.
Hence write down the value of T_4 .

Different ways to reach the 4th step:	$1 + 1 + 1 + 1$
<p>Answer: $T_4 = \underline{\hspace{2cm}}$</p>	

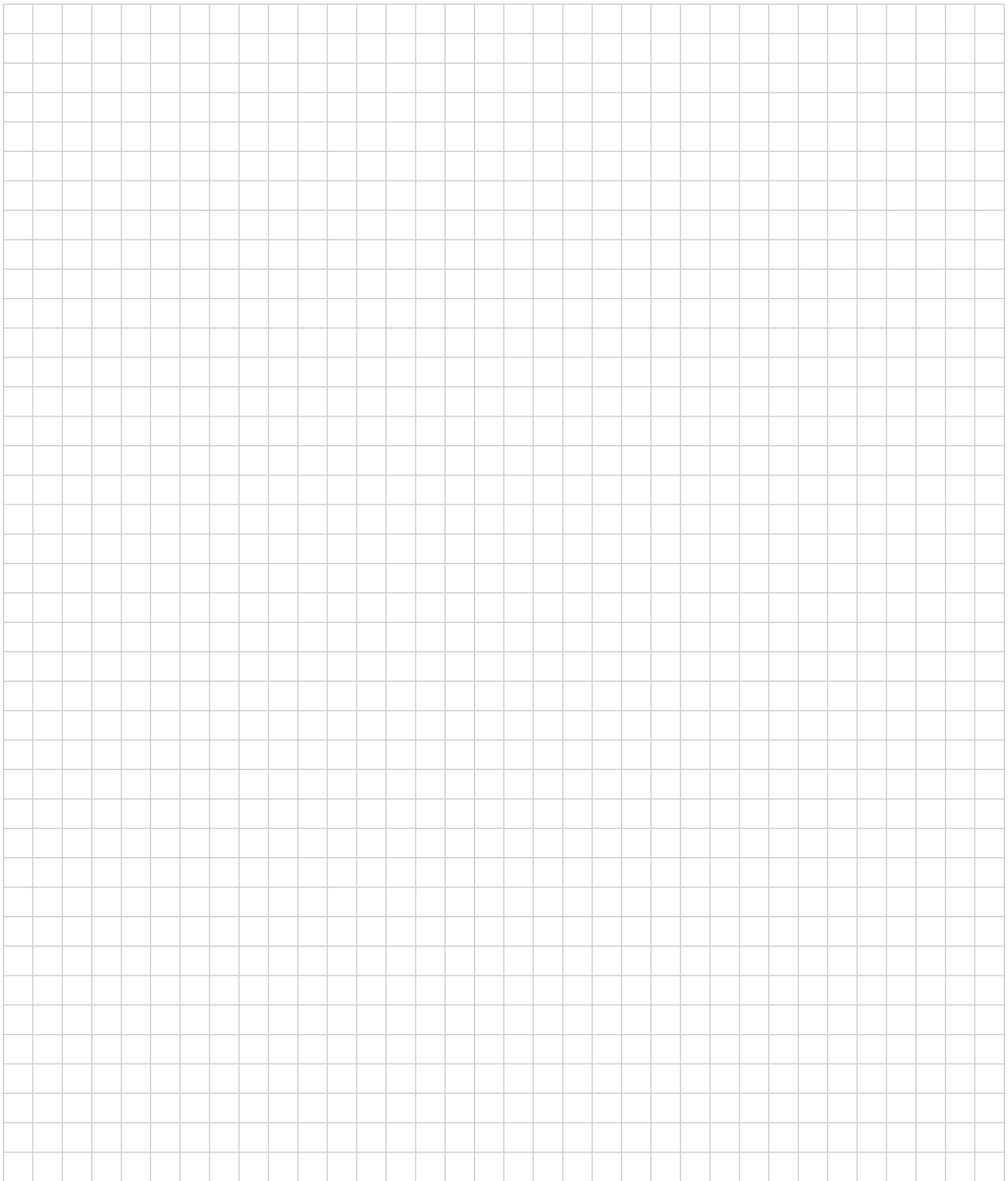
Some of the ways to reach the n th step start by going up **1 step**; others start by going up **2 steps**.

(c) (i) List the different ways that she can reach the 5th step, if she starts by going up **1 step**.

(ii) List the different ways that she can reach the 5th step, if she starts by going up **2 steps**.

(d) Explain why $T_{100} = T_{99} + T_{98}$.

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