

AN ROINN OIDEACHAIS.  
(Department of Education).

BRAINNSE AN MHEADHON-OIDEACHAIS  
(Secondary Education Branch).

LEAVING CERTIFICATE EXAMINATION, 1938.

PASS.  
MATHEMATICS  
(ALGEBRA)

TUESDAY, 21st JUNE.—AFTERNOON, 3.30 TO 6 P.M.

Seven questions may be answered.

Mathematical Tables may be obtained from the Superintendent.

1. Find the common factor of  $3x^3 - 11x^2 - 24x + 20$  and  $2x^3 - 3x^2 - 30x - 25$ .

Solve the equations

(i)  $3x^3 - 11x^2 - 24x + 20 = 0$ ,

(ii)  $2x^3 - 3x^2 - 30x - 25 = 0$ .

[25 marks.]

2. Prove that  $(a+b+c)^n - a^n - b^n - c^n$  is divisible by  $b+c$  when  $n$  is an odd positive integer.

Factorise  $(a+b+c)^3 - a^3 - b^3 - c^3$ .

[25 marks.]

3. If  $a + \frac{1}{a} = k$ , express  $a^2 + \frac{1}{a^2}$  and  $a^2 - \frac{1}{a^2}$  in terms of  $k$ .

[25 marks.]

4. A man purchased a certain quantity of coal at a certain price. If it were five shillings a ton cheaper he would have got two tons more for the money, but if it were three shillings a ton dearer he would have got one ton less. Find the number of tons purchased and the cost price per ton.

[25 marks.]

5. Express the square root of  $57 - 12\sqrt{15}$  in the form  $a\sqrt{x} - b\sqrt{y}$ , where  $a, b, x, y$  are rational quantities.

[25 marks.]

6. Solve the simultaneous equations

$$\left. \begin{aligned} (x+y)^2 + 2(x+y) &= 15 \\ (x-y)^2 - 4(x-y) &= 12 \end{aligned} \right\}$$

[30 marks.]

7. AD is a perpendicular of an equilateral triangle ABC; EF is a perpendicular of an equilateral triangle ADE; GH is a perpendicular of an equilateral triangle EFG and so on. Prove that the sides of those triangles are in Geometrical Progression and find the common ratio.

If BC is *one foot* in length determine which one of the triangles is the first to have a side not more than *one inch* in length.

[30 marks.]

8. Insert  $n$  Arithmetic Means between  $a$  and  $b$  and find the sum of those Means.

Show that the sum of the  $n$  Arithmetic Means and the sum of the  $m$  Arithmetic Means between  $a$  and  $b$  are in the ratio  $n : m$ .

[30 marks.]

9. ABC is a triangle which is right-angled at C, and CD is the perpendicular from C on AB. Prove that  $AB \cdot CD = CA \cdot CB$  and calculate the length of AB when  $CD = 12$  inches,  $BC + CA = 35$  inches.

[30 marks.]

10. Using the same axes and the same scales draw graphs of  $5+x-x^2(=y)$  and  $\frac{3-x}{1+x}(=y)$ ;

Using your graphs determine approximately

(a) the maximum value of  $5+x-x^2$ ,

(b) the roots of the equation  $(1+x)(5+x-x^2)=3-x$ .

[30 marks.]