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LEAVING CERTIFICATE EXAMINATION, 1935.

PASS.

MATHEMATICS
(GEOMETRY)

FRIDAY, 14th JUNE.—MORNING, 10 A.M. TO 12.30 P.M.

Six questions may be answered.

Mathematical Tables may be obtained from the Superintendent.

Candidates should state the text-book used in order to indicate the sequence followed.

1. P is a point outside a circle: show how to find points, X and Y on the circle such that PX and PY shall be tangents.

Prove that $PX = PY$.

[33 marks.]

2. M is the mid-point of the side AB of a triangle ABC: prove that $CA^2 + CB^2 = 2(AM^2 + MC^2)$.

X and Y are points within a circle: show how to find a point Z on the circumference such that $ZX^2 + ZY^2$ may be as small as possible.

[33 marks.]

3. From a point Q outside a circle lines QAB and QCD are drawn intersecting the circle at A, B, C, D: prove that $QA \cdot QB = QC \cdot QD$.

Two circles intersect at M and N; prove that tangents drawn to the circles from any point on the line MN produced are equal.

[33 marks.]

4. AB is the diameter of a semicircle ACB; from any point P on AB a line, PC, is drawn perpendicular to AB: prove that $AP \cdot PB = PC^2$.

If $AB = 12$ ins. and $AP + PC = 14$ ins., calculate the length of AP.

[33 marks.]

5. The bisector of the angle BAC of a triangle ABC meets BC at D: prove that $AB:AC = BD:DC$.
State and prove the converse theorem.

[33 marks.]

6. Show how to find a point P on a line AB produced such that $PA \cdot PB = AB^2$.

Construct accurately a triangle whose angles are in the ratios 1:2:2 and whose shortest side is 3 ins. long. Explain your construction.

[The use of the *Protractor* is not allowed.]

[33 marks.]

7. Show that a line drawn parallel to one side of a triangle divides the other sides in equal ratios.

EFGH is the inscribed circle of the square ABCD whose side = $2s$; another circle of radius x ins. touches EFGH externally and the sides AB, BC internally. Prove that $x = s(\sqrt{2}-1)^2$.

[33 marks.]

8. Prove that for a triangle ABC, $\frac{a}{\sin A} = 2R$, where R = the radius of the circumcircle.

The angles of a triangle are in arithmetical progression and the diameter of the circumcircle is 20 ins. Prove that one of the angles of the triangle contains 60° and show that the opposite side is $10\sqrt{3}$ ins long.

[34 marks.]

9. Two small boats, X and Y, are anchored in a harbour. A, B, C are points on the strand such that A, B, C, X, Y all lie in the same plane; A, B, X are collinear and A, C, Y are collinear. Calculate the distance between X and Y when $AB = 150$ yds., $AC = 200$ yds. angle $XBY = 64^\circ 53'$, angle $XAY = 50^\circ$, angle $XCY = 72^\circ 31'$.

[34 marks.]