AN ROINN OIDEACHAIS

(Department of Education.)

INTERMEDIATE CERTIFICATE EXAMINATION, 1942.

ELEMENTARY MATHEMATICS (Geometry). FOR GIRLS ONLY.

WEDNESDAY, 10th JUNE .- MORNING, 10 to 11.30.

Six questions may be answered.

All questions carry equal marks.

Mathematical Tables may be obtained from the Superintendent.

1. Show, with proof, how to bisect an angle geometrically.

2. What is meant by an isosceles triangle?

On opposite sides of BC as base two isosceles triangles ABC, DBC are constructed. Prove that AD bisects BC perpendicularly.

3. PQR is a triangle in which PQ is greater than PR: prove that the angle PRQ is greater than the angle PQR.

If S is any point in the side QR, prove that the angle PSQ is greater than the angle PQR.

4. On a line XY two points B, C are marked such that BC=3.6 ins. and a triangle ABC is constructed having BA=3.2 ins., CA=2 ins. Find (i) the locus of the points which are 1 inch from XY, (ii) all the points which are 3 ins. from A and 1 inch from XY.

5. Prove that the angle in a semi-circle is a right angle.

Two circles intersect at A and B. AC and AD are two diameters, one in each circle. Show that the points C, B, D are in one straight line.

6. PQR is a triangle and L is the mid-point of PQ. Through L a line is drawn parallel to QR and meeting PR at M. Prove that M is the mid-point of PR.

ABCD is a quadrilateral in which AB is parallel to DC. From E, the mid-point of AD, a line is drawn parallel to AB meeting BC at F. Prove that F is the mid-point of BC.

7. Prove that if the square on one side of a triangle is equal to the sum of the squares on the other two sides the triangle is right-angled.

The lengths, in inches, of the sides of four triangles are as follows: (i) 4, 7, 8; (ii) 5, 4, 3; (iii) 13, 12, 5; (iv) 11, 8, 7. Find whether any of those triangles are right-angled.

[Do not construct these triangles.]

8. Show how to draw a tangent to a circle from a point outside the circle. Prove your construction.

Calculate the length of the tangent drawn to a circle 2 ins, in radius from a point 5 ins, from the centre of the circle.

9. Construct accurately a quadrilateral ABCD such that AB=AC=4 ins., BC= $2\frac{1}{2}$ ins., AD=3 ins., \angle ADC=90°.

Construct geometrically a triangle equal in area to ABCD. [Explain your construction fully.]